

Master-Abschlussvortrag

Distributed Wavelet Tree Construction

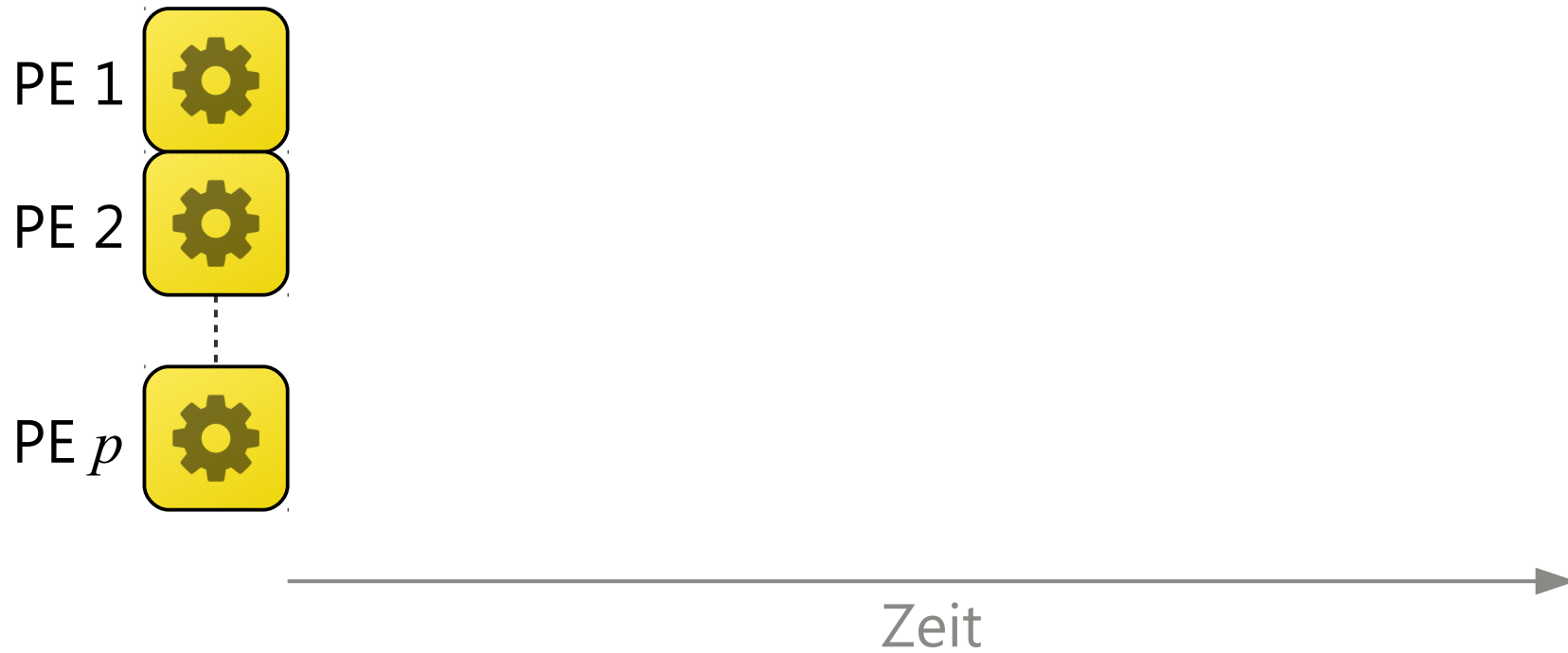
Patrick Dinklage

Gutachter:

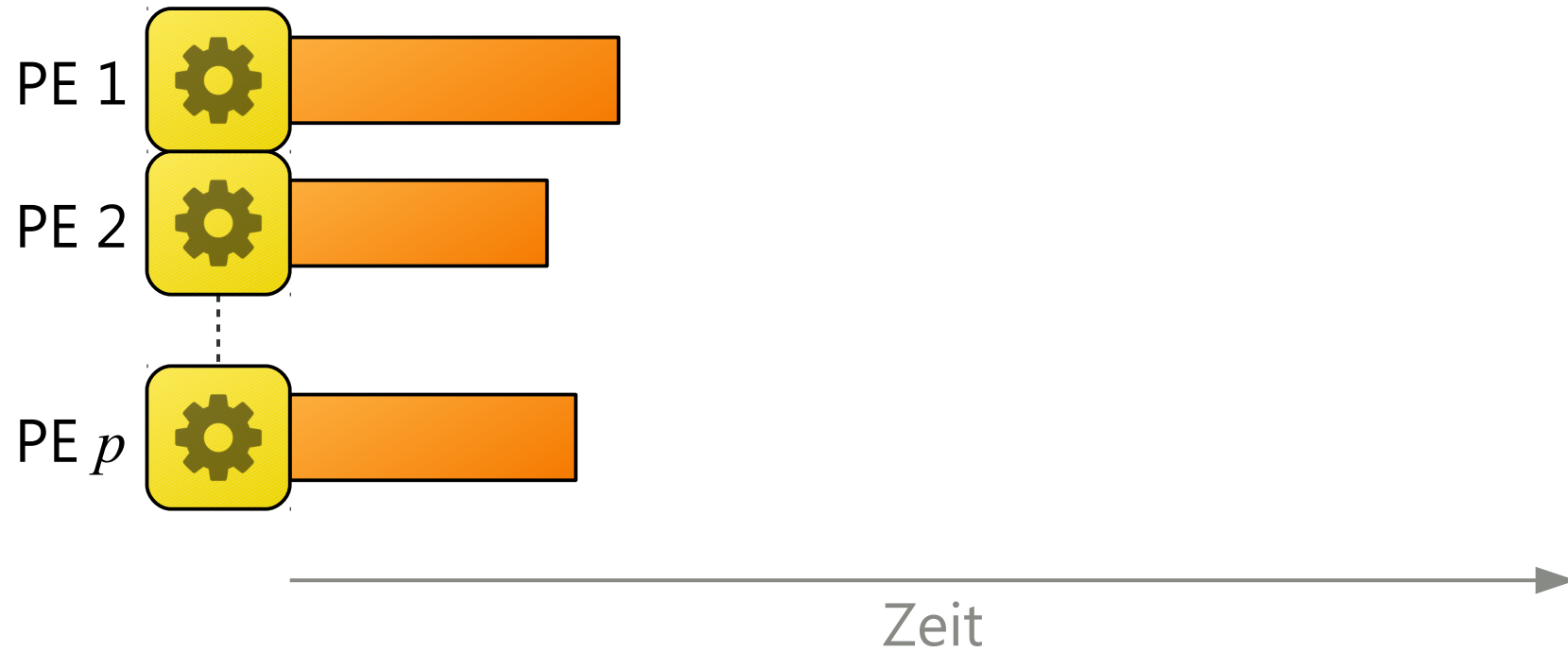
Prof. Dr. Johannes Fischer

M. Sc. Florian Kurpicz

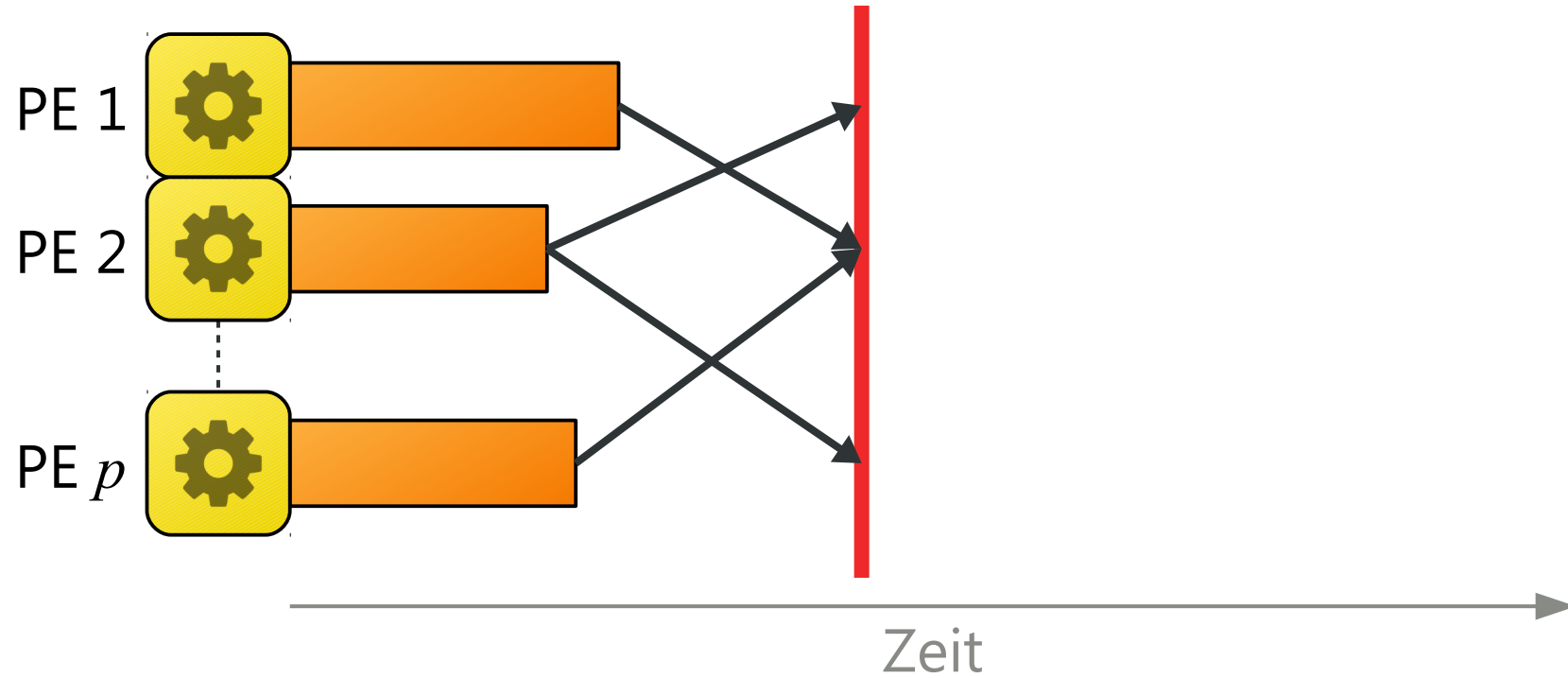
Das BSP-Modell



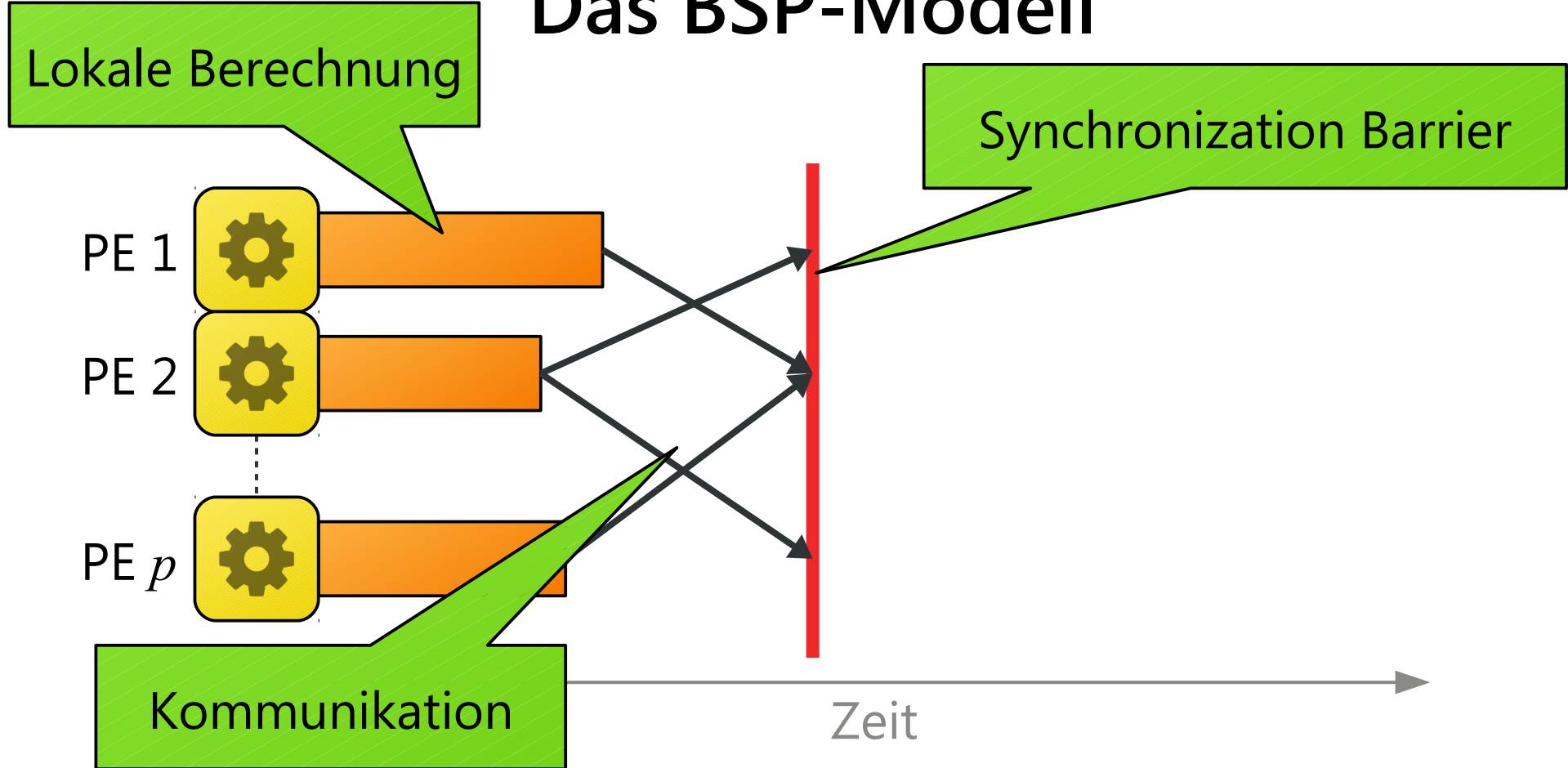
Das BSP-Modell



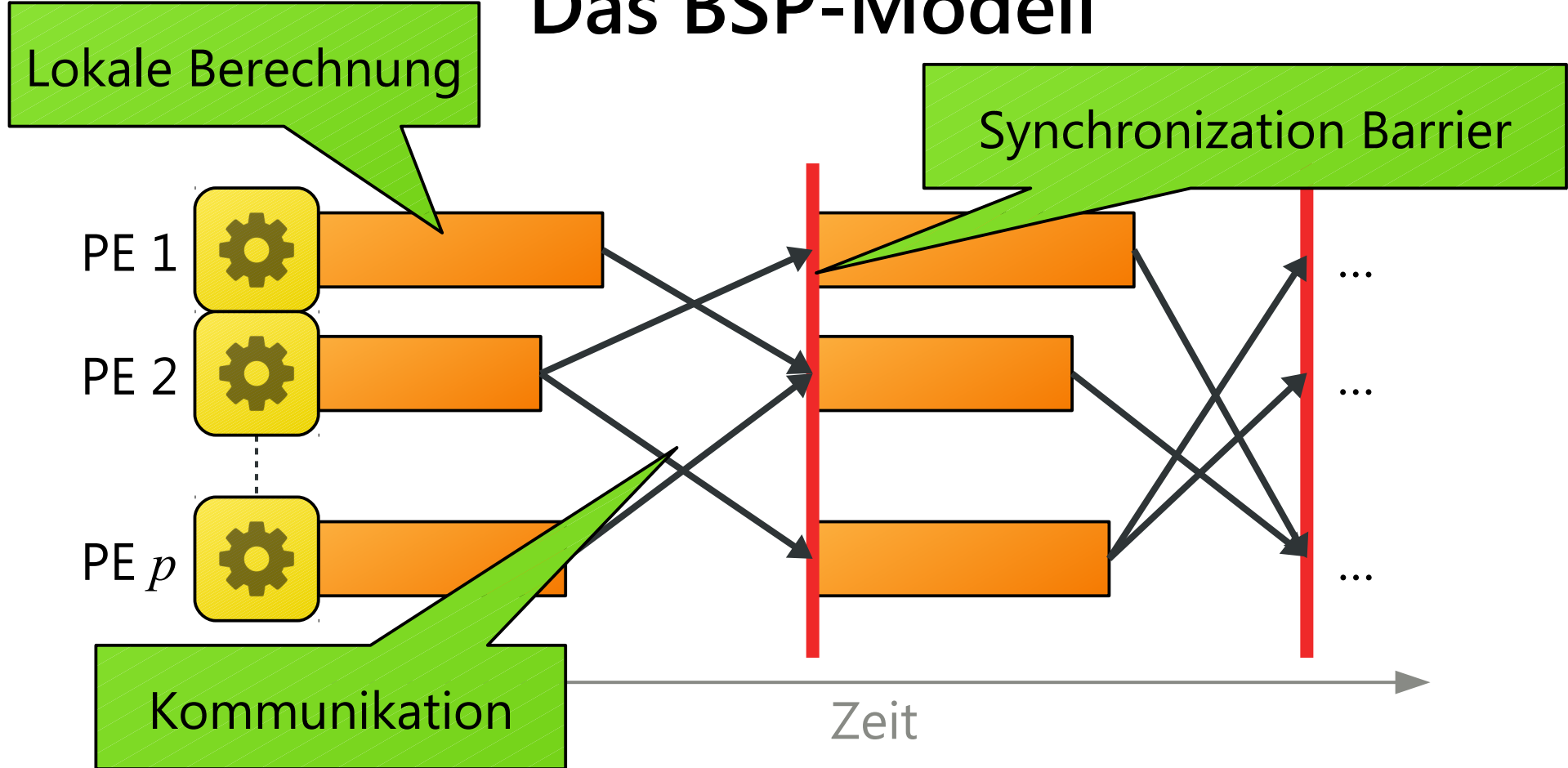
Das BSP-Modell



Das BSP-Modell



Das BSP-Modell



BSP-Kostenanalyse



Anzahl lokaler Berechnungsschritte



Anzahl versendeter Computerwörter



Anzahl Synchronization Barrier

Wavelet Trees

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wavelettree
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Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$

wavelettree

Wavelet Trees

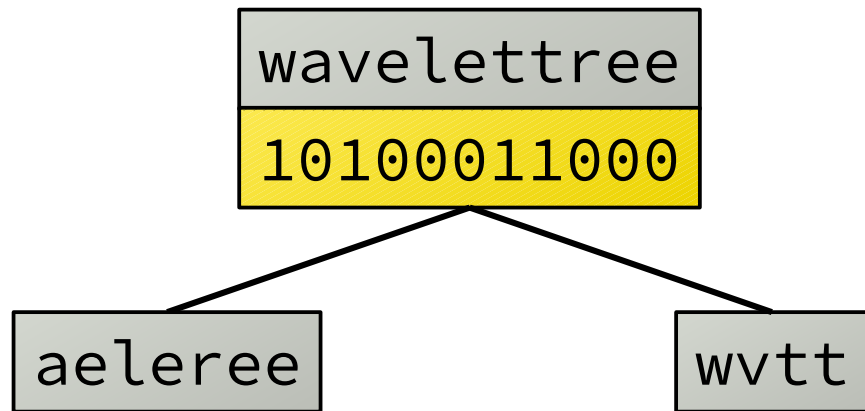
$\Sigma = \{a, e, l, r, t, v, w\}$

wavelettrees

10100011000

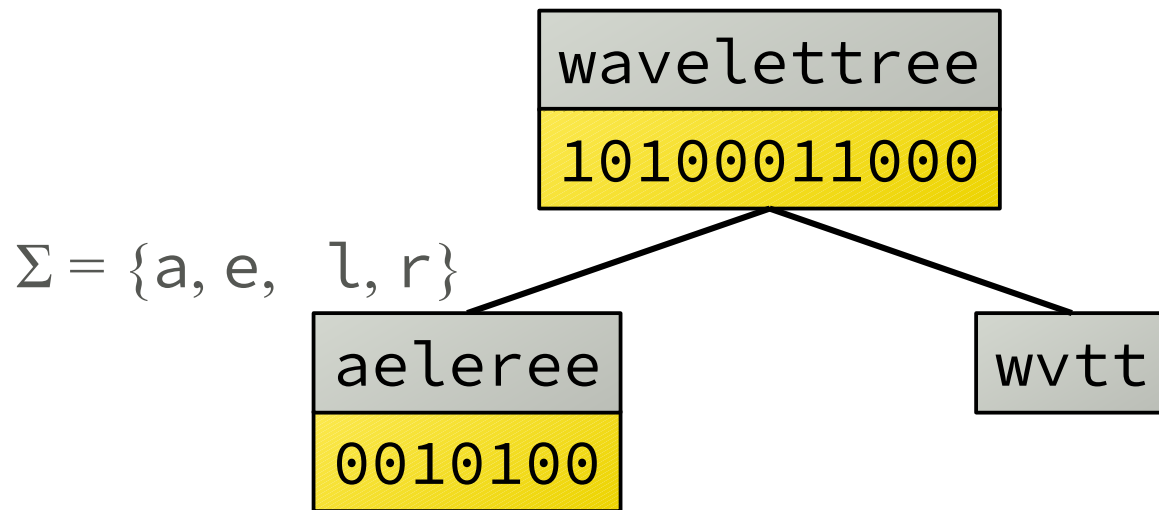
Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



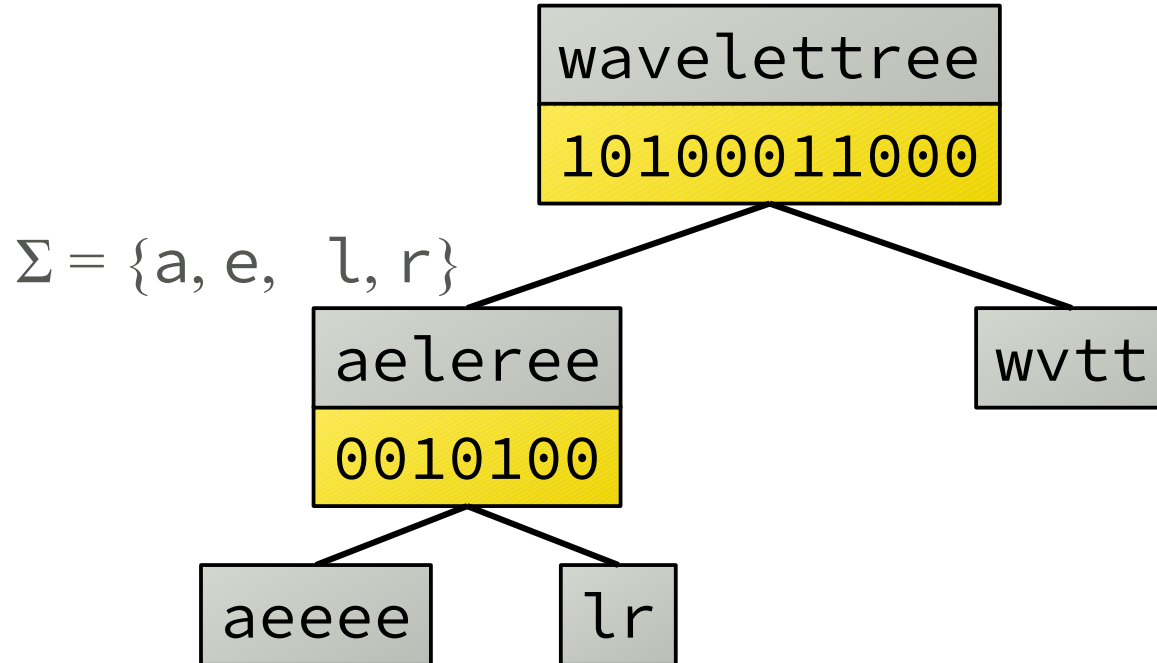
Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



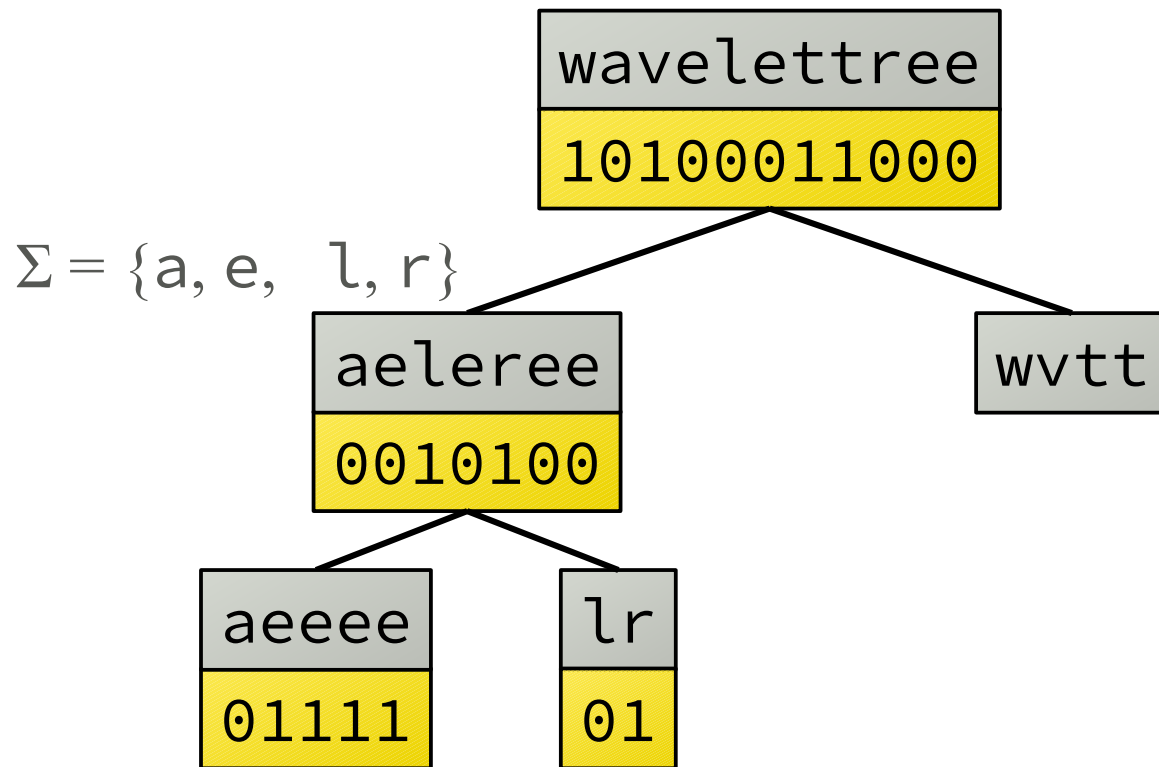
Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



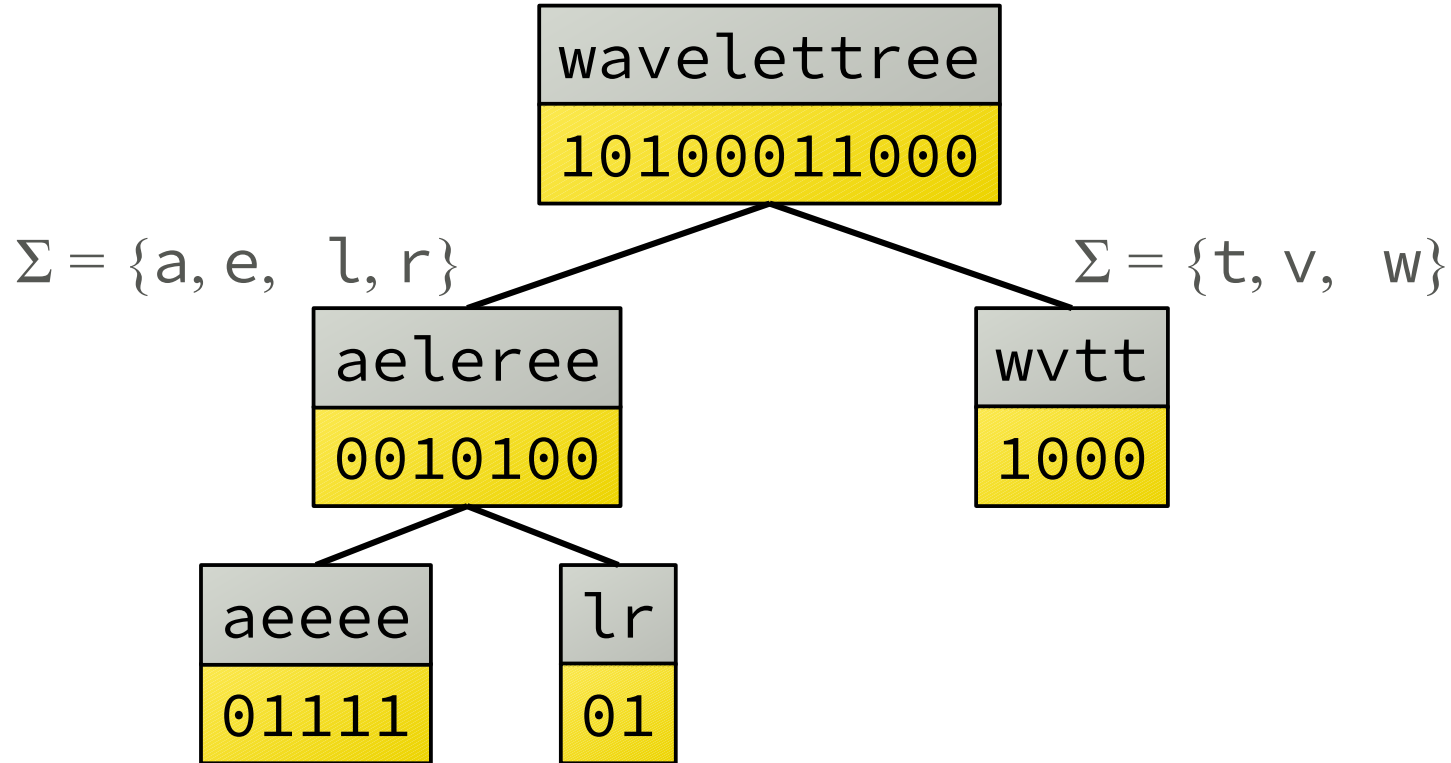
Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



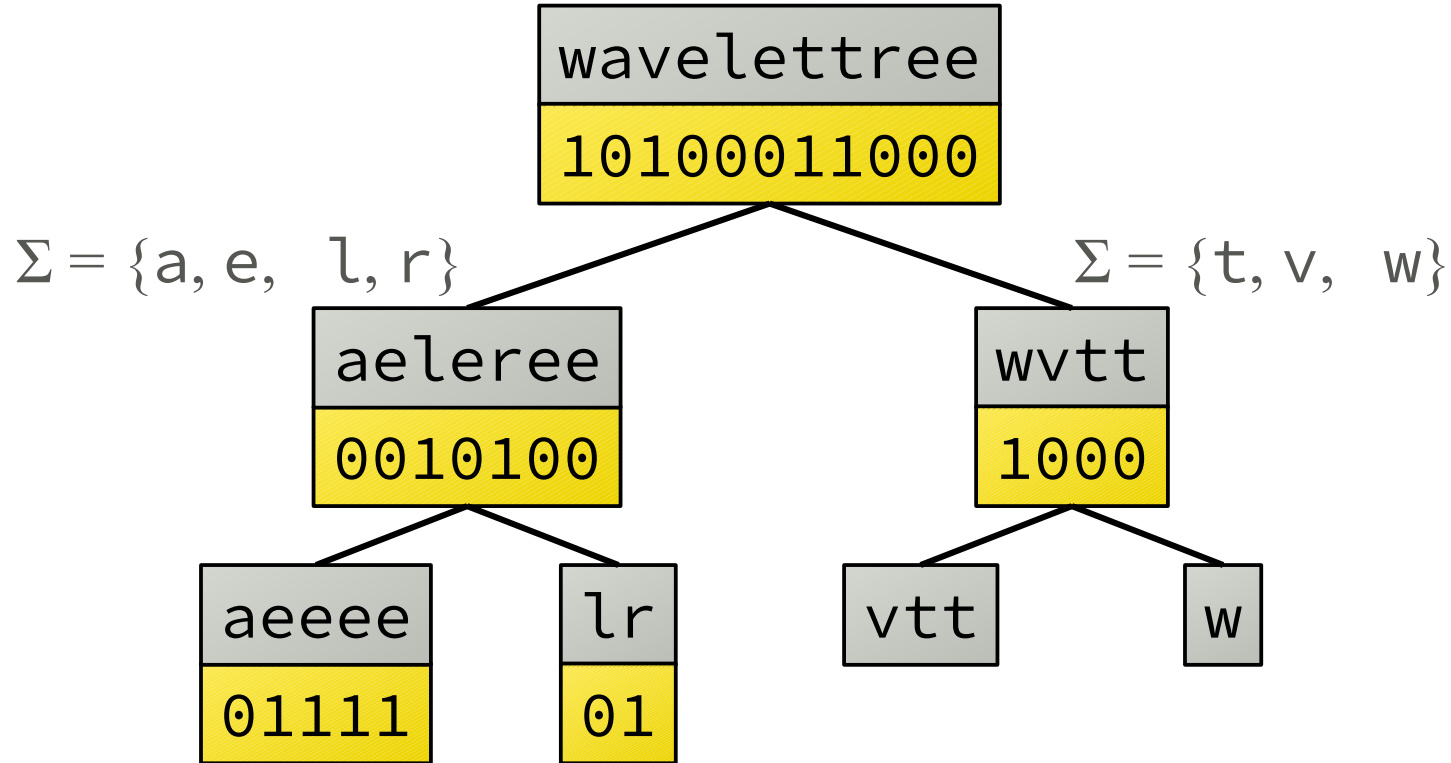
Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



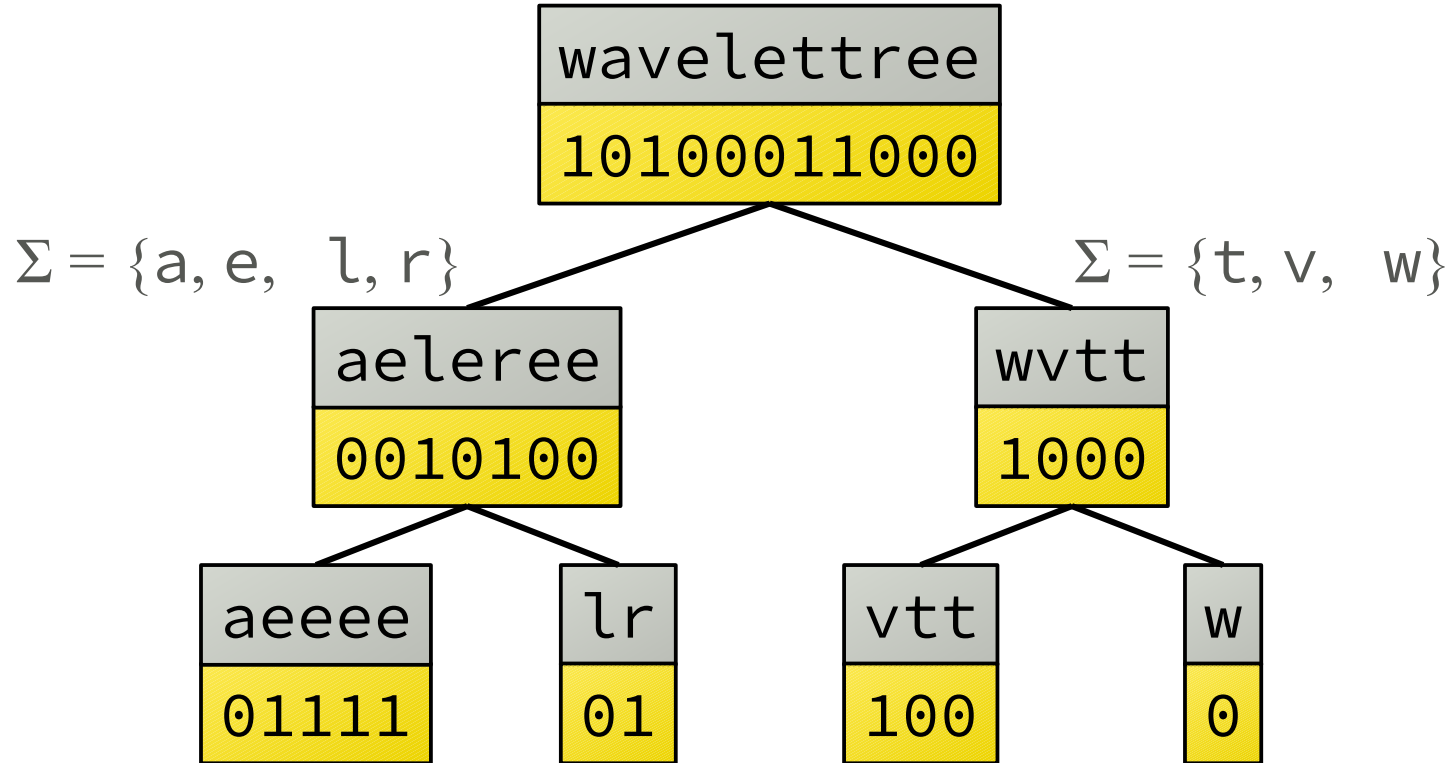
Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



Wavelet Trees

$\Sigma = \{a, e, l, r, t, v, w\}$



Wavelet Trees

Levelweise Darstellung

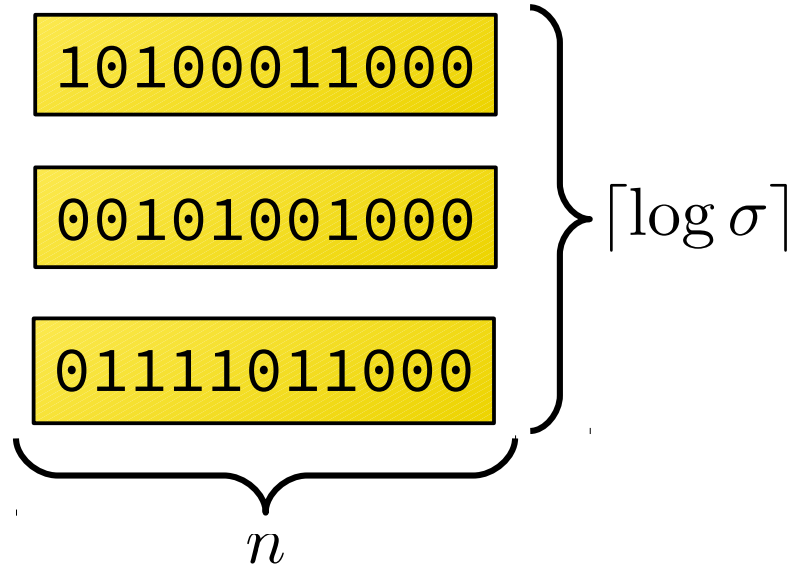
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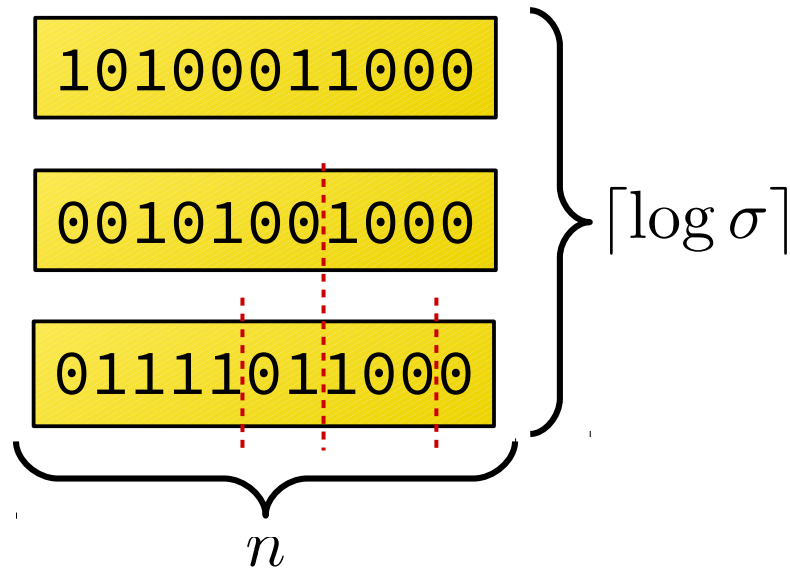
Wavelet Trees

Levelweise Darstellung



Wavelet Trees

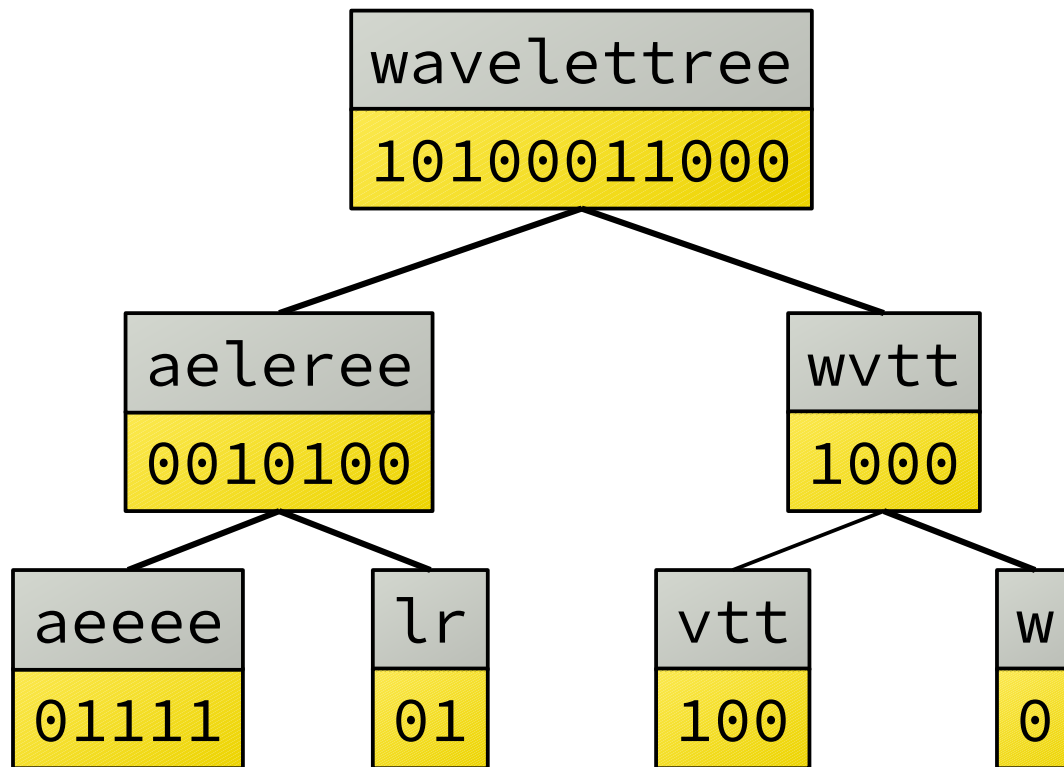
Levelweise Darstellung



+ rank/select je Level

Wavelet Trees

Bit-Pfade



Wavelet Trees

Bit-Pfade

Effektives Alphabet:

$a \mapsto 0 = 000_b$

$e \mapsto 1 = 001_b$

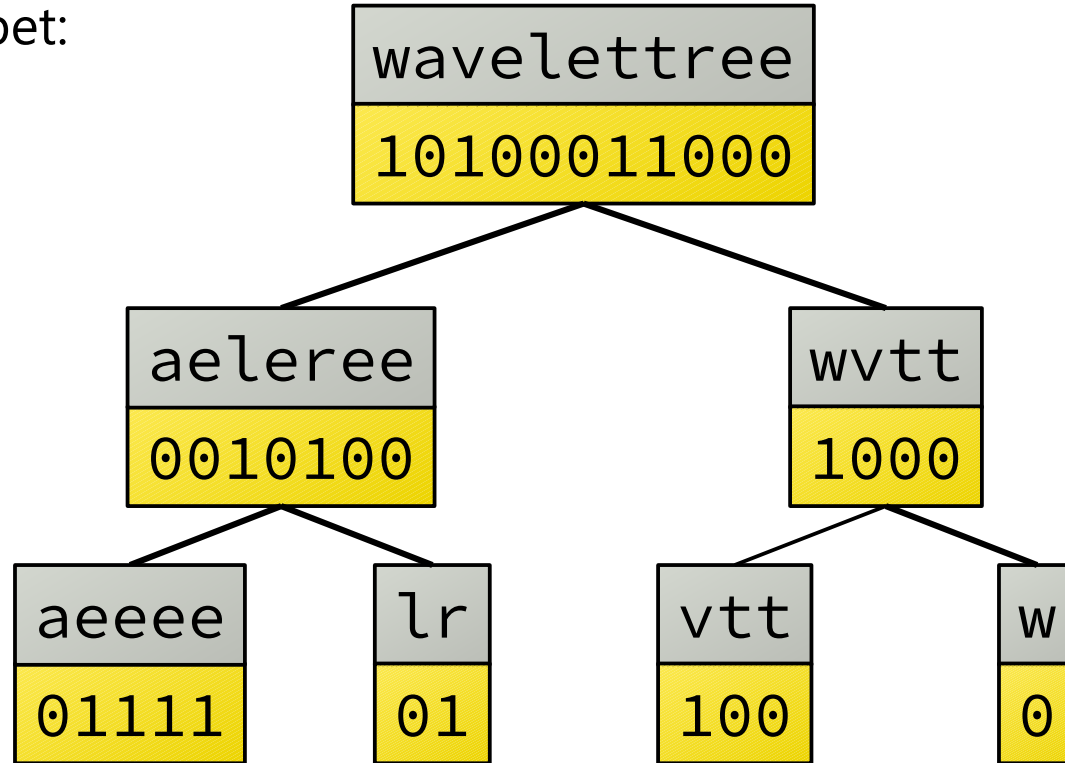
$l \mapsto 2 = 010_b$

$r \mapsto 3 = 011_b$

$t \mapsto 4 = 100_b$

$v \mapsto 5 = 101_b$

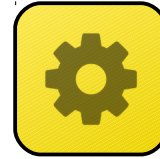
$w \mapsto 6 = 110_b$



Verteile Wavelet-Tree-Konstruktion

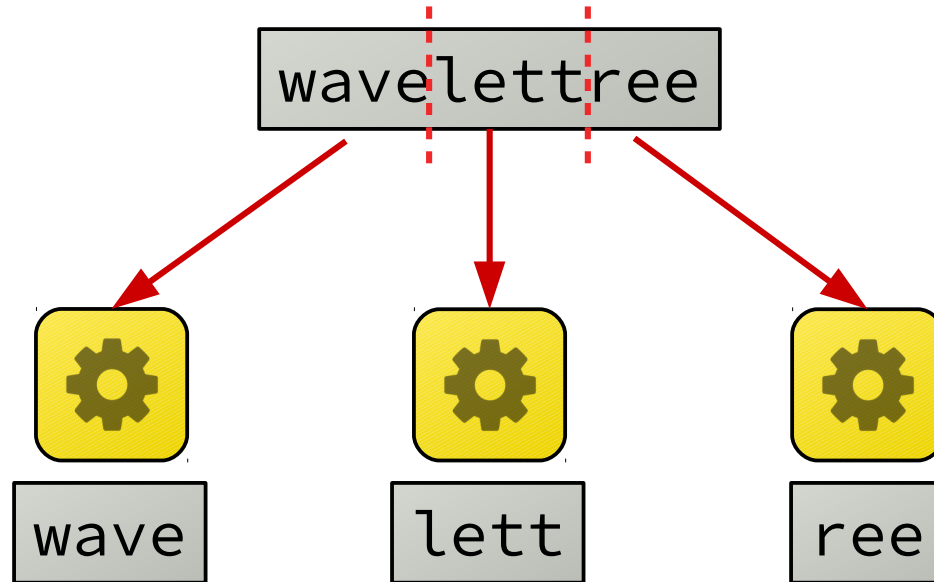
Partitionierung der Eingabe

wavelettree



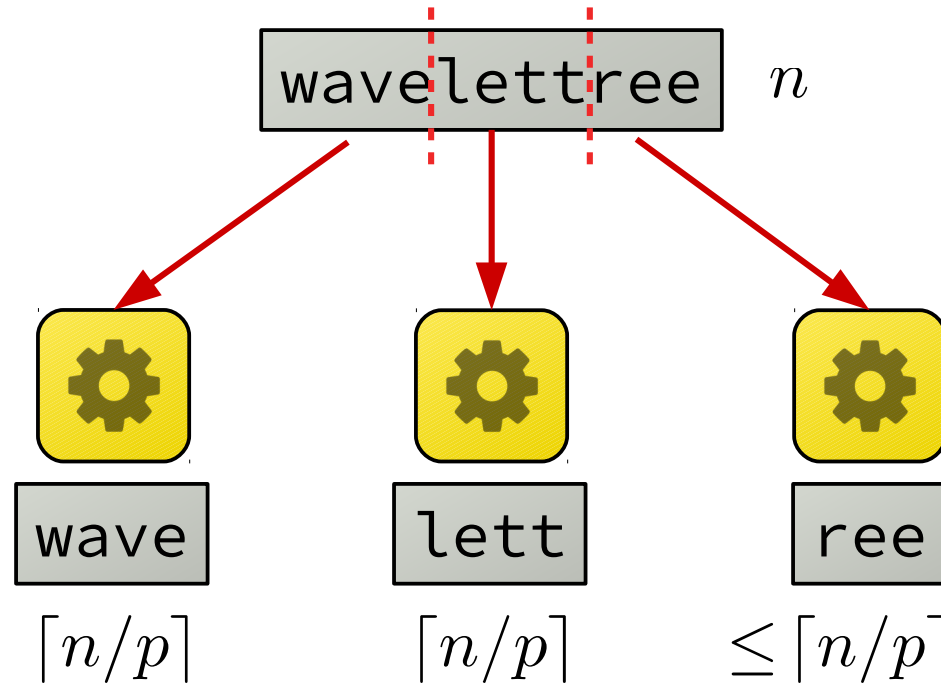
Verteile Wavelet-Tree-Konstruktion

Partitionierung der Eingabe



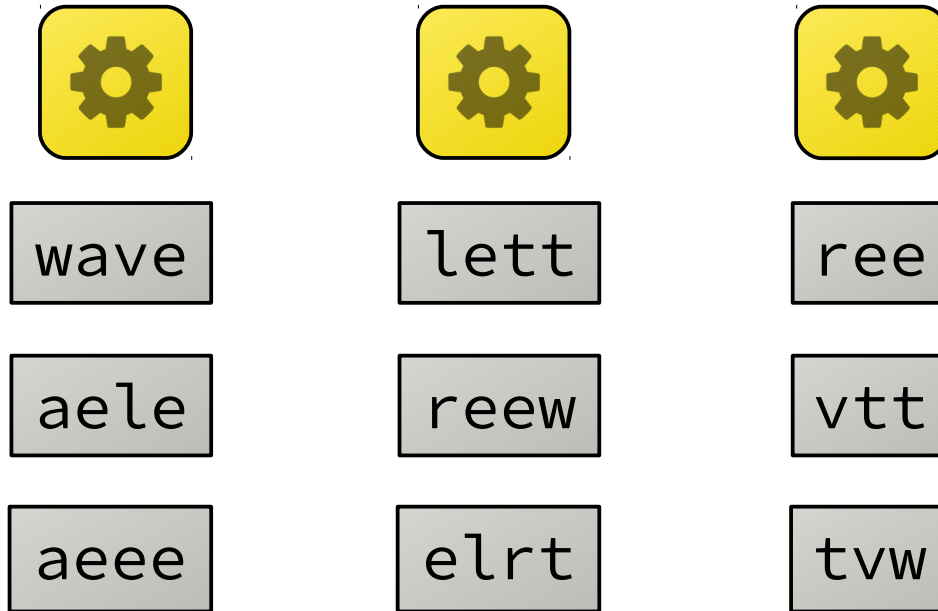
Verteile Wavelet-Tree-Konstruktion

Partitionierung der Eingabe



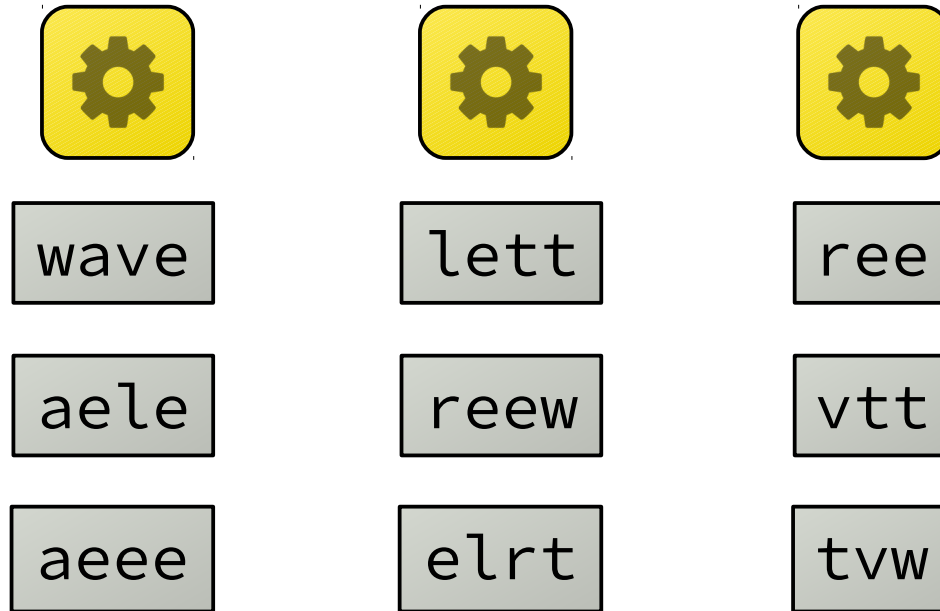
Verteile Wavelet-Tree-Konstruktion

Ausgabeformat



Verteile Wavelet-Tree-Konstruktion

Ausgabeformat



→ Partitionierte levelweise Darstellung

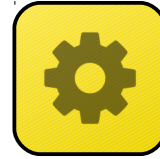
Domain Decomposition



wave

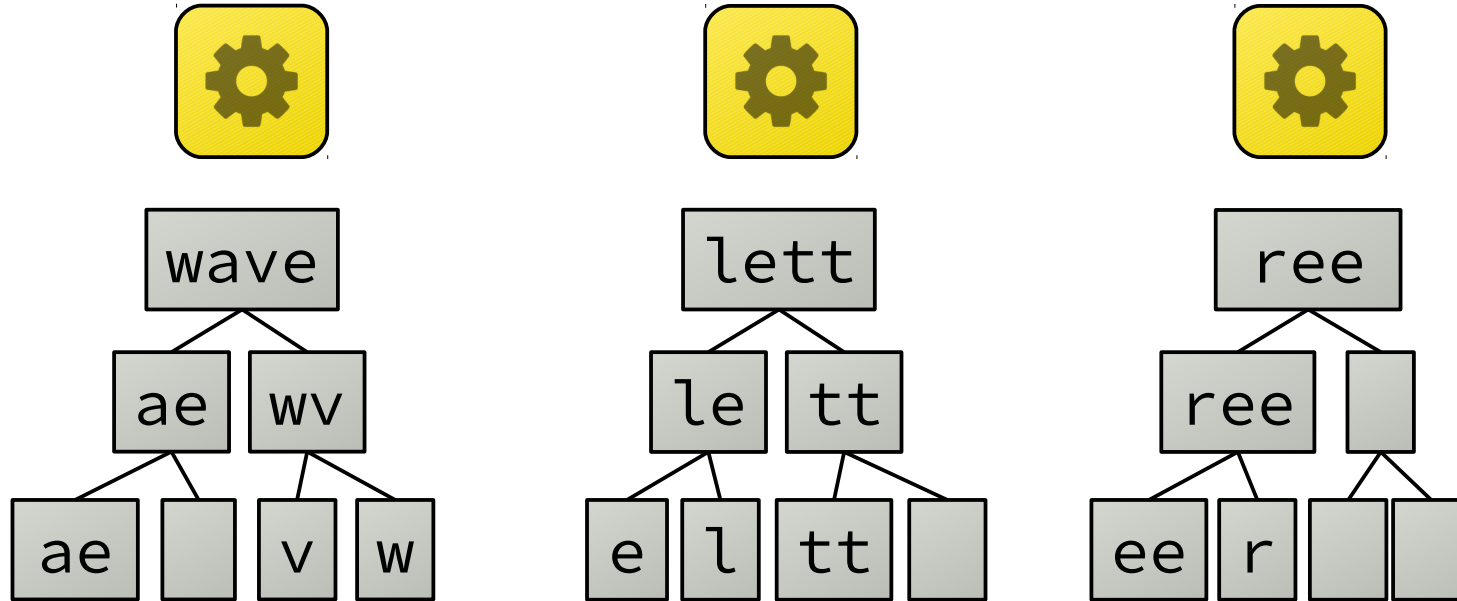


lett

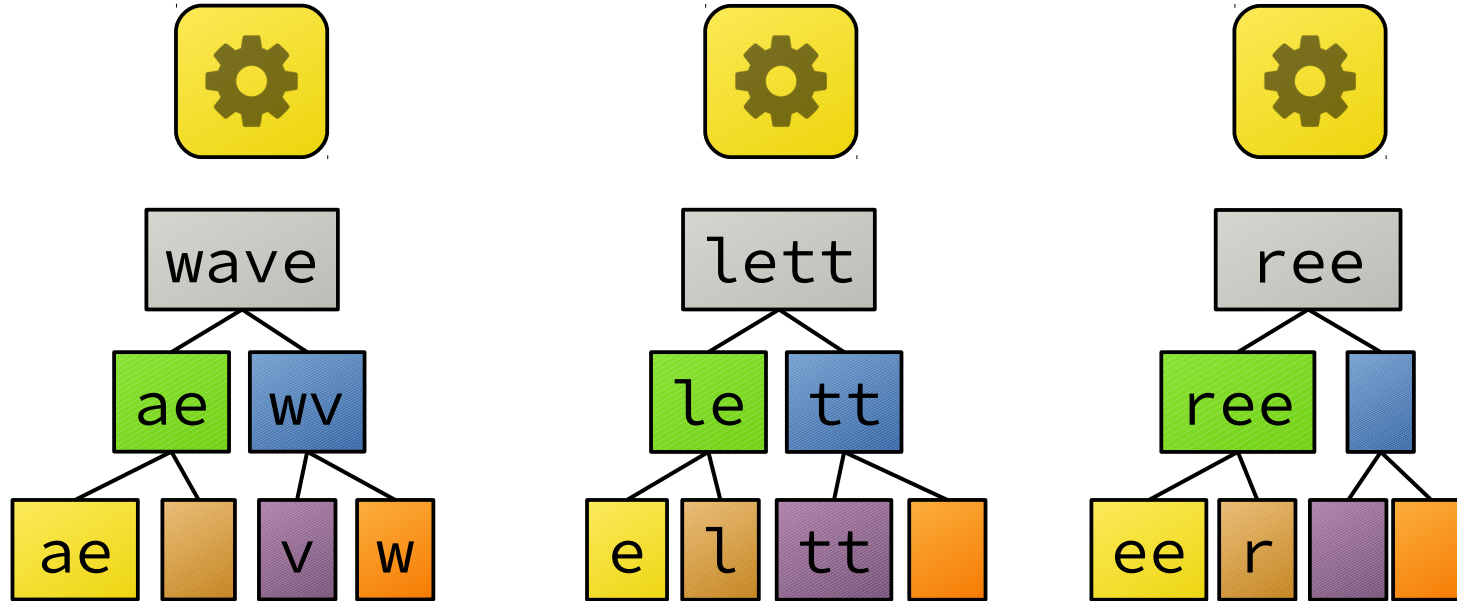


ree

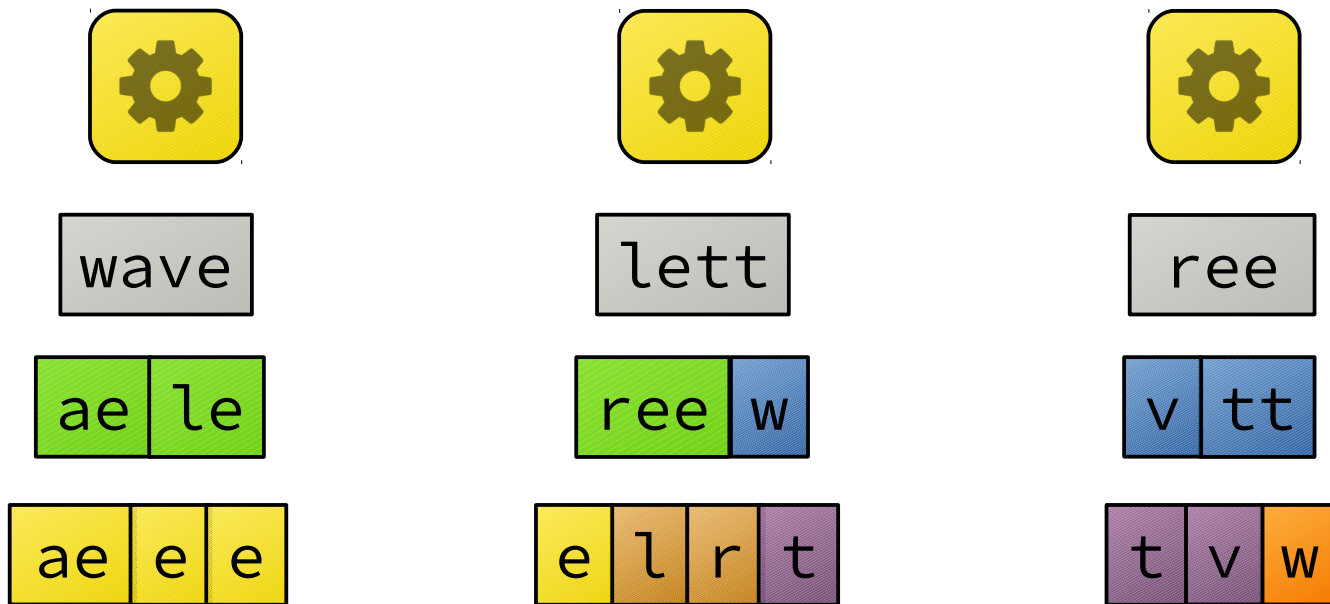
Domain Decomposition



Domain Decomposition



Domain Decomposition



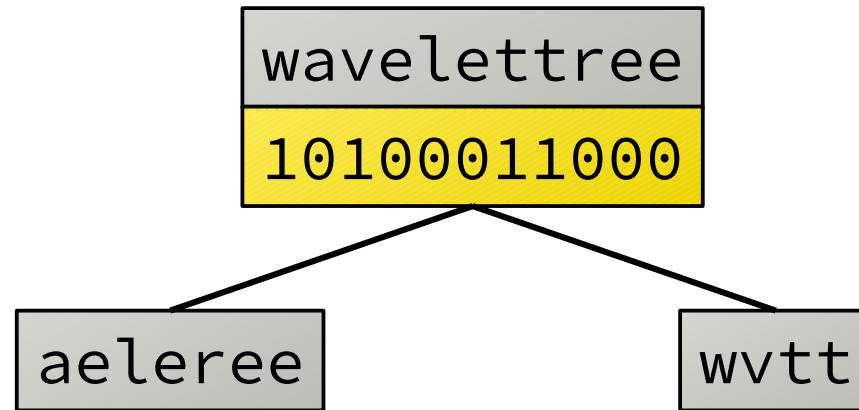
Verteiltes Aufsplitten

wavelettree

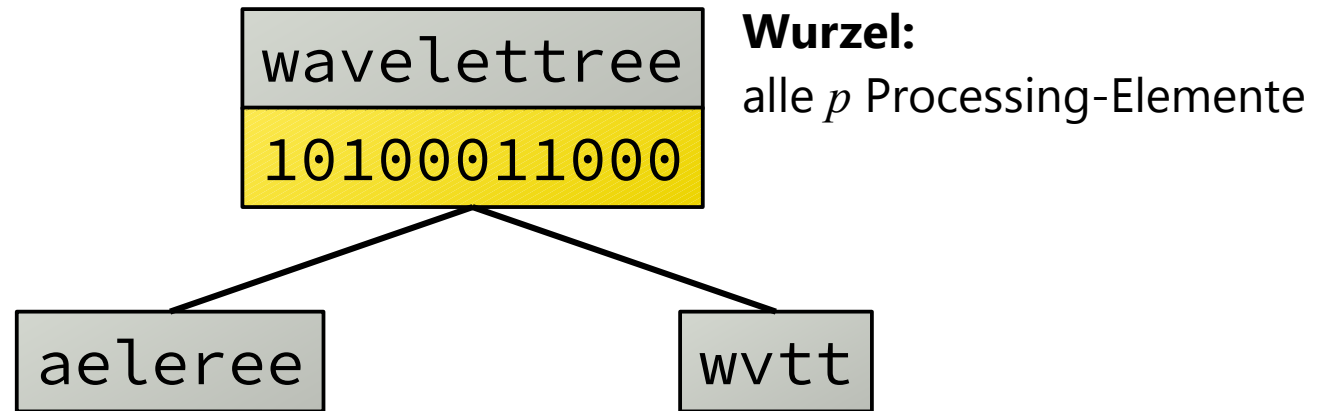
Verteiltes Aufsplitten

wavelettree
10100011000

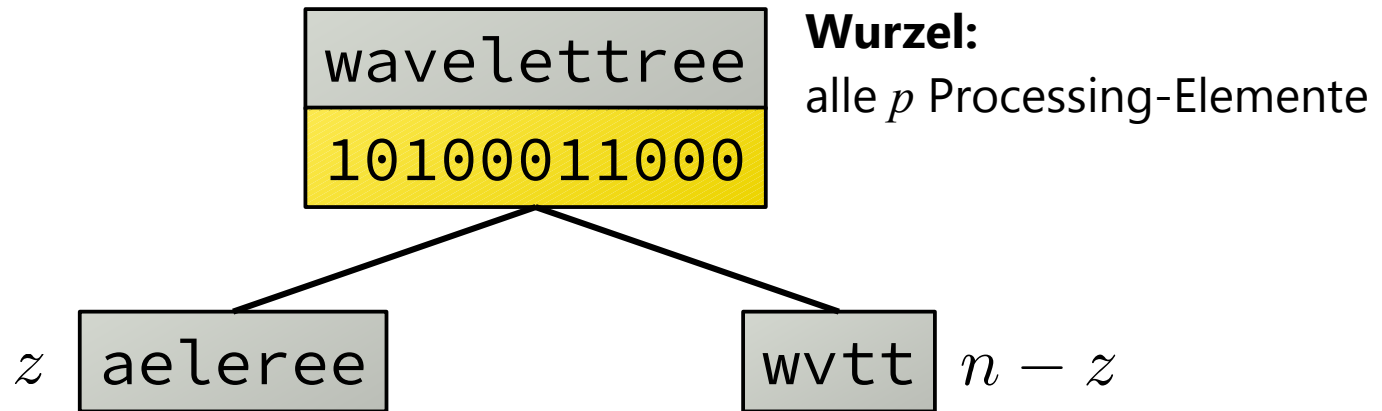
Verteiltes Aufsplitten



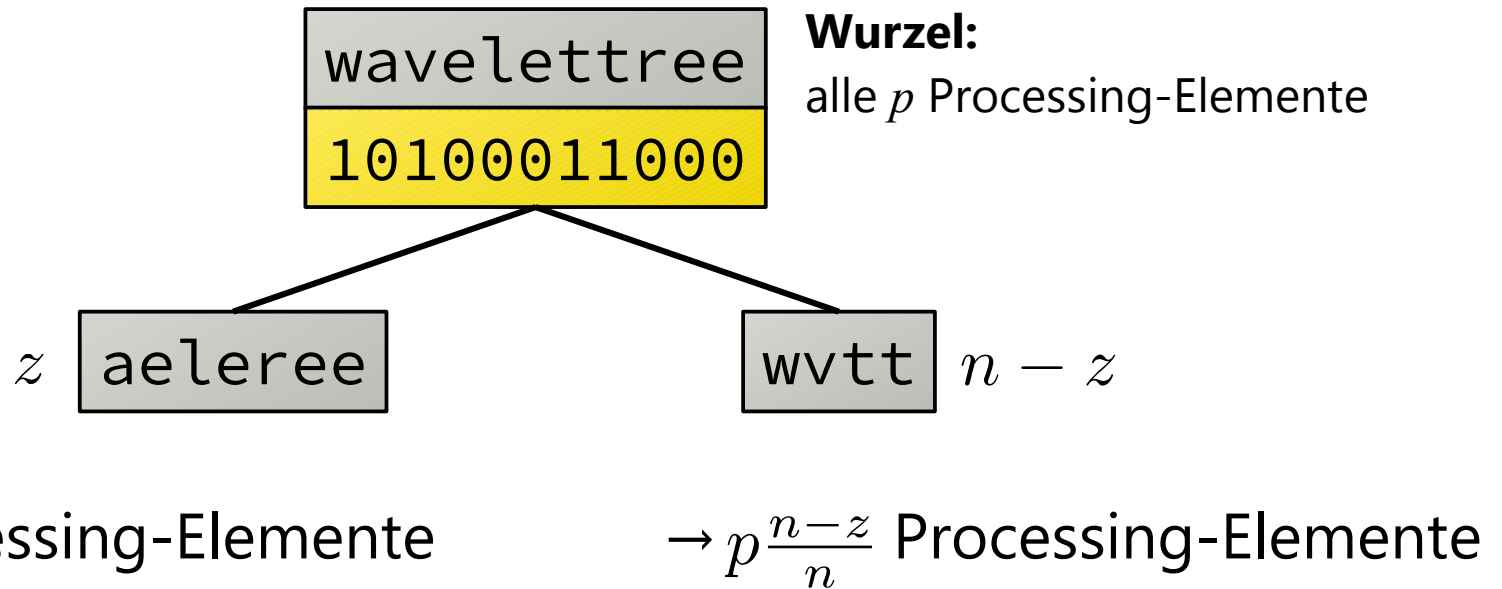
Verteiltes Aufsplitten



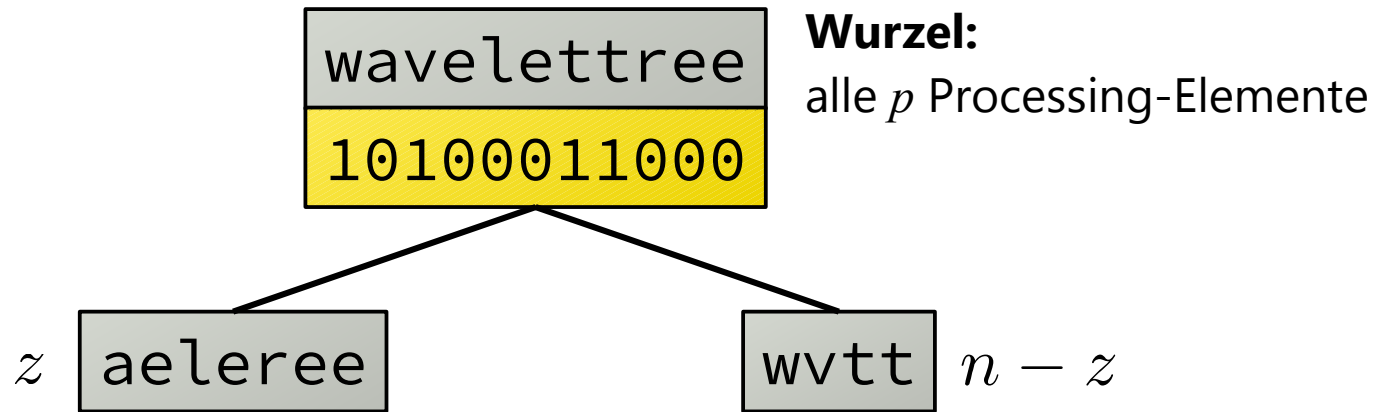
Verteiltes Aufsplitten



Verteiltes Aufsplitten



Verteiltes Aufsplitten



→ $p \frac{z}{n}$ Processing-Elemente

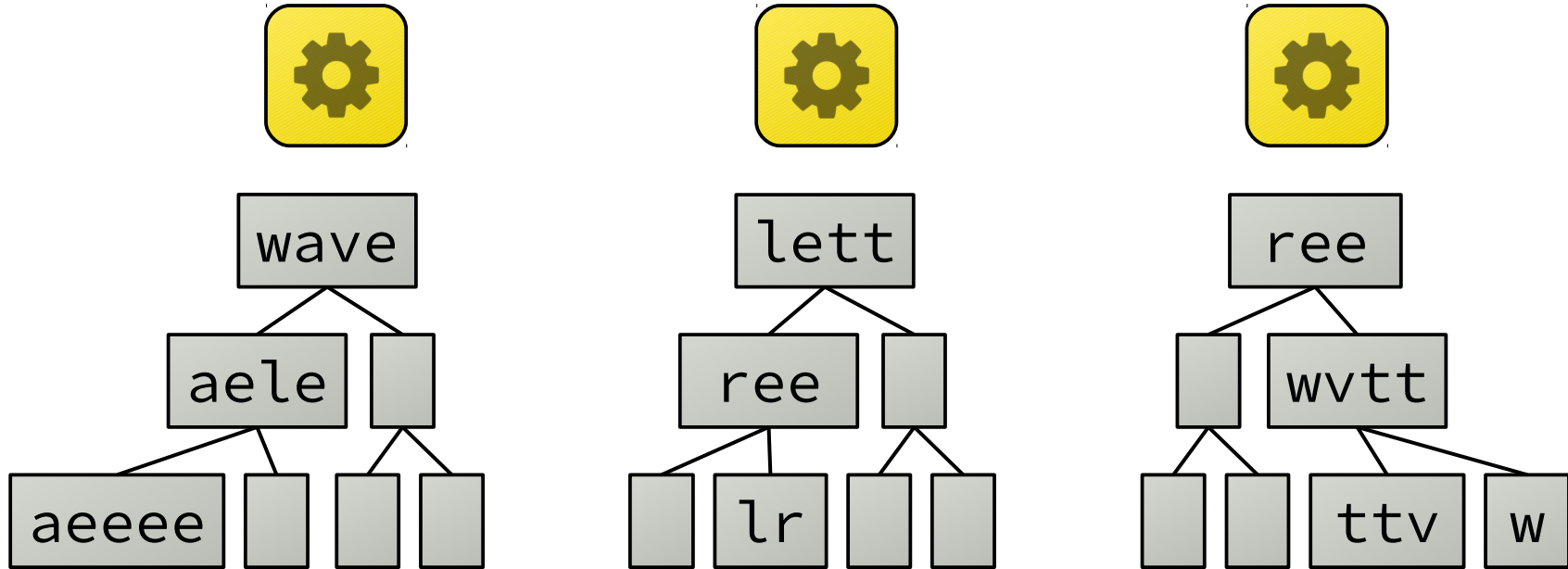
$$z = 7 \Rightarrow \frac{z}{n} \approx \frac{2}{3} \rightarrow 2 \text{ PEs}$$

→ $p \frac{n-z}{n}$ Processing-Elemente

$$\frac{n-z}{n} \approx \frac{1}{3} \rightarrow 1 \text{ PE}$$

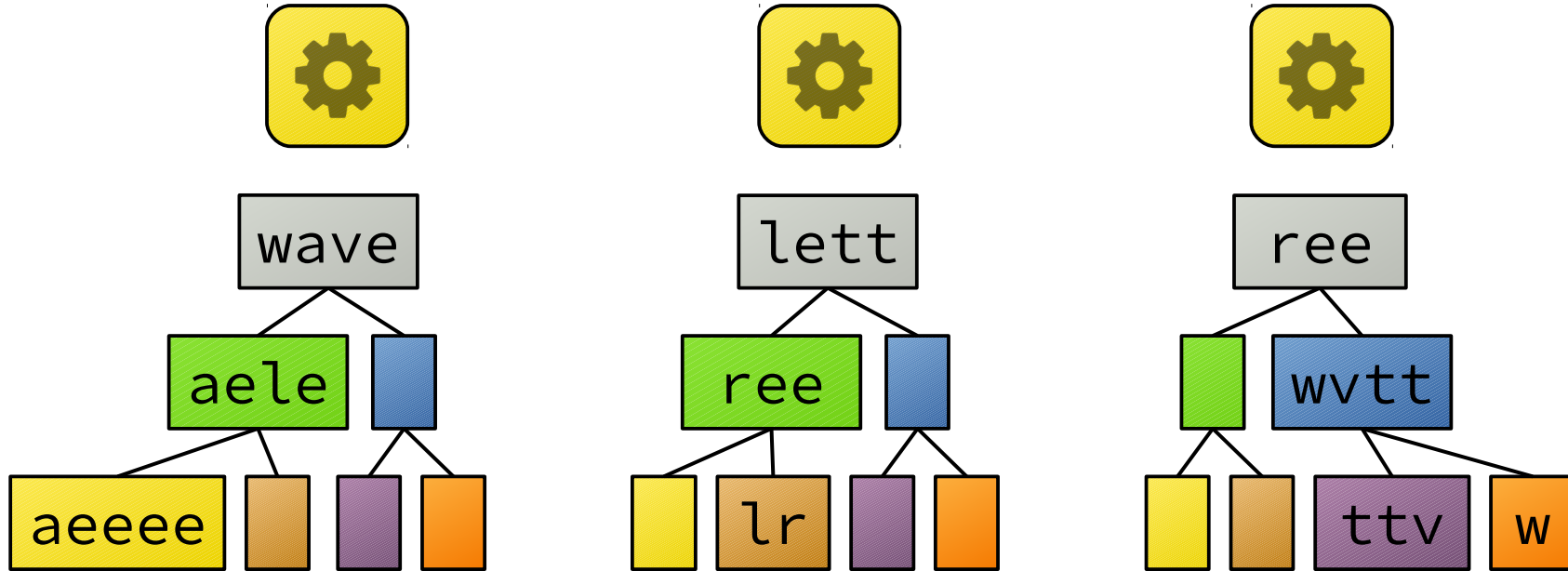
Verteiltes Aufsplitten

Merge



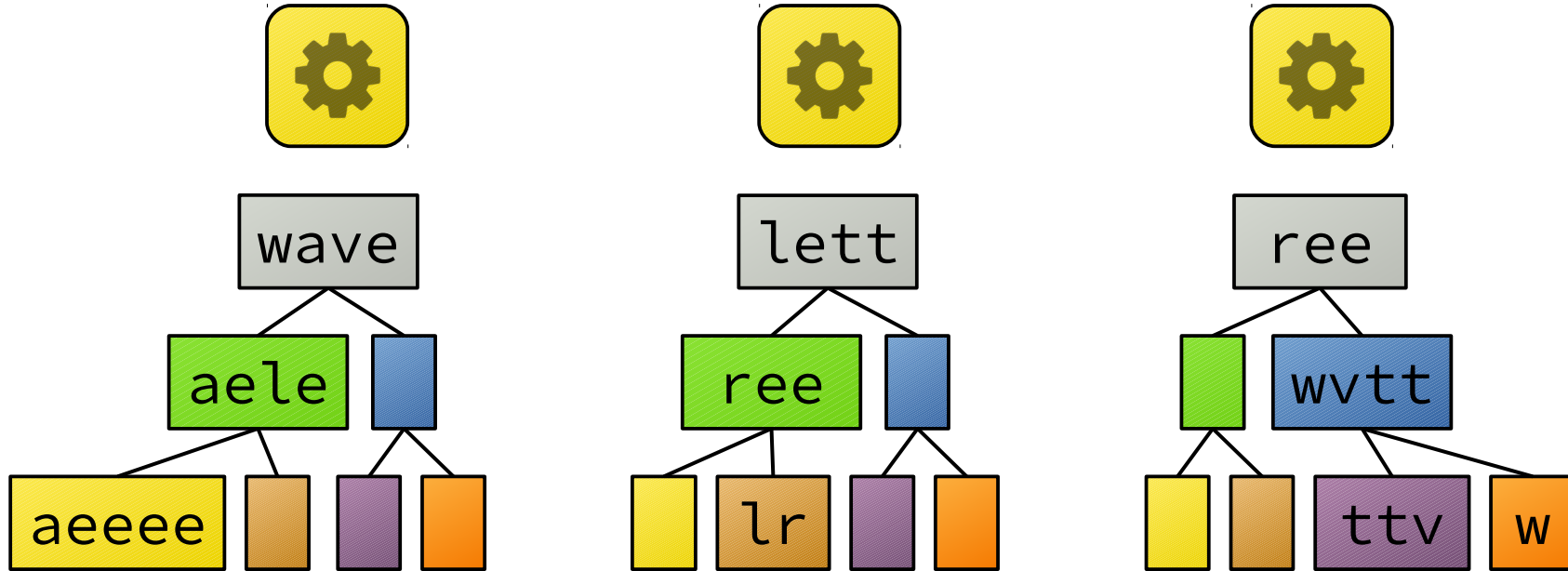
Verteiltes Aufsplitten

Merge



Verteiltes Aufsplitten

Merge



→ Variante des Szenarios bei der Domain Decomposition!

Stabiles Sortieren

wavelettree

Stabiles Sortieren

wavelettree

Effektives Alphabet:

$a \mapsto 0 = 000_b$

$e \mapsto 1 = 001_b$

$l \mapsto 2 = 010_b$

$r \mapsto 3 = 011_b$

$t \mapsto 4 = 100_b$

$v \mapsto 5 = 101_b$

$w \mapsto 6 = 110_b$

Stabiles Sortieren

w	a	v	e	l	e	t	t	r	e	e
110	000	101	001	010	001	100	100	011	001	001

Effektives Alphabet:

$a \mapsto 0 = 000_b$

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Stabiles Sortieren

w	a	v	e	l	e	t	t	r	e	e
110	000	101	001	010	001	100	100	011	001	001

Effektives Alphabet:

$a \mapsto 0 = 000_b$

$e \mapsto 1 = 001_b$

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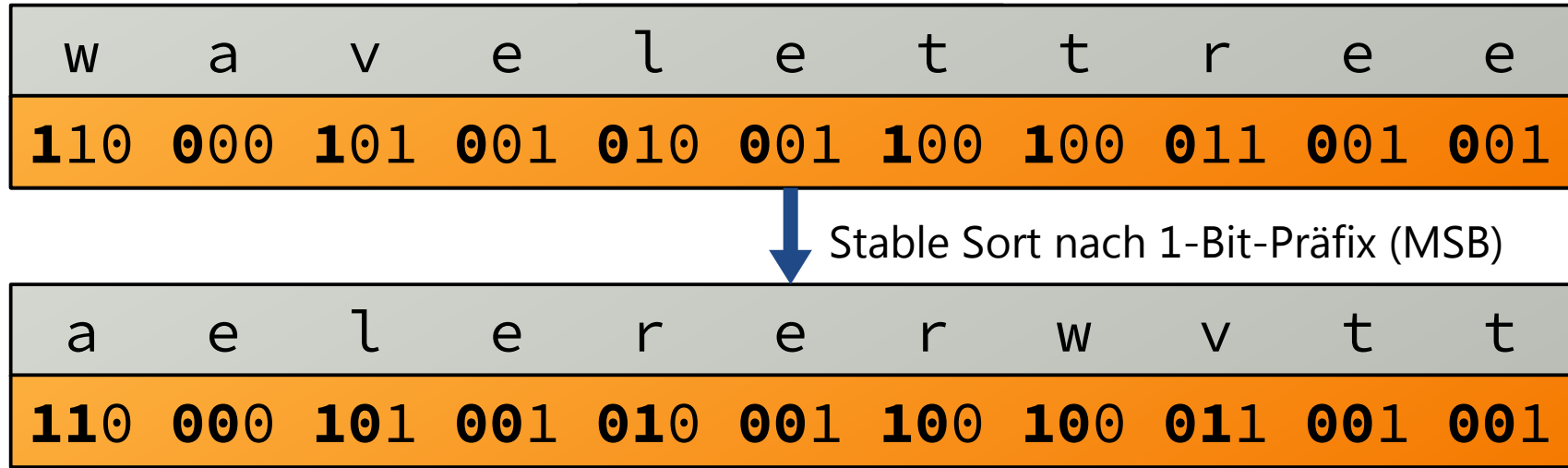
$r \mapsto 3 = 011_b$

$t \mapsto 4 = 100_b$

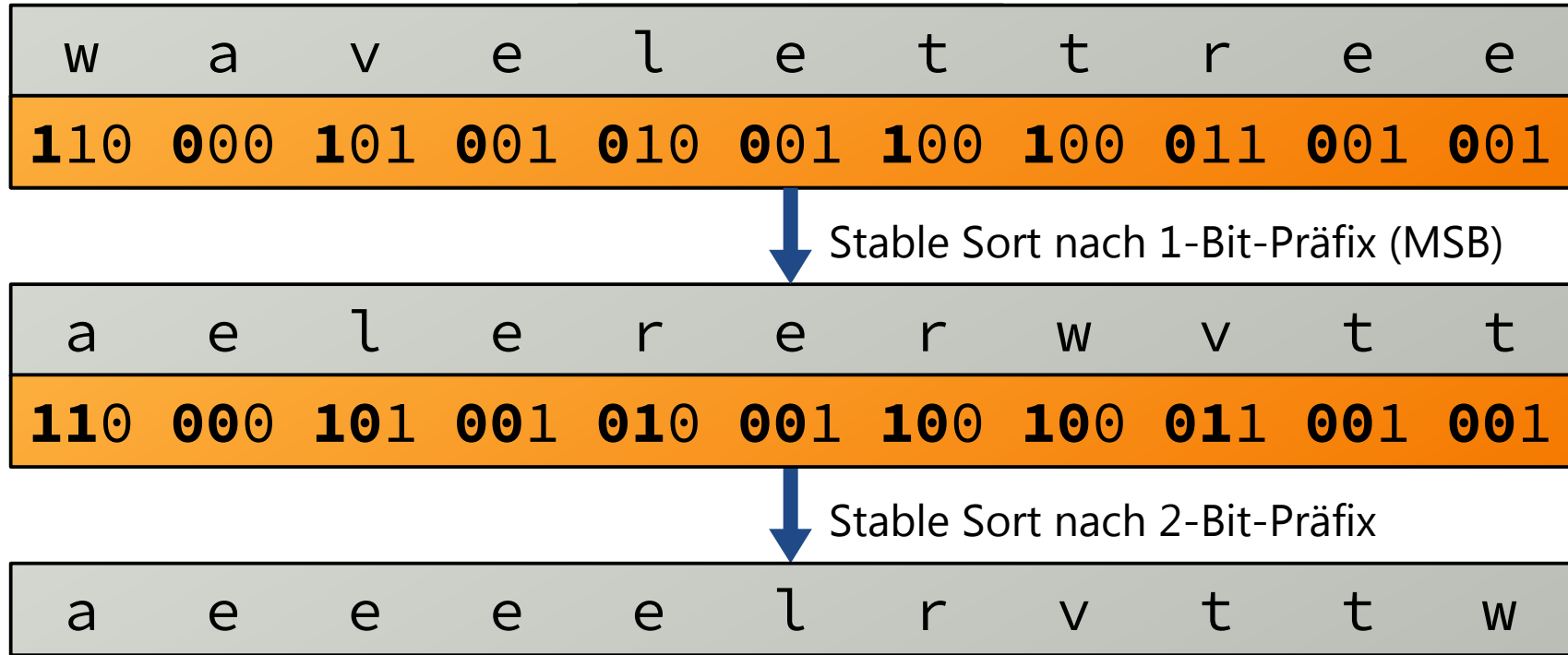
$v \mapsto 5 = 101_b$

$w \mapsto 6 = 110_b$

Stabiles Sortieren



Stabiles Sortieren



Stabiles Sortieren

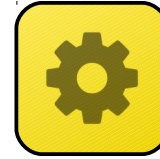
Verteilter Bucket Sort



wave



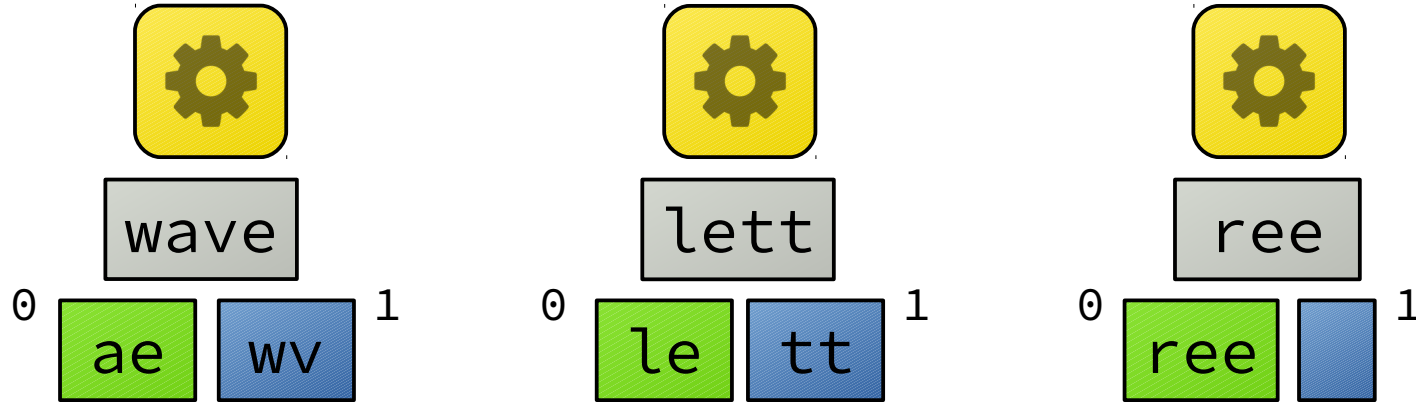
lett



ree

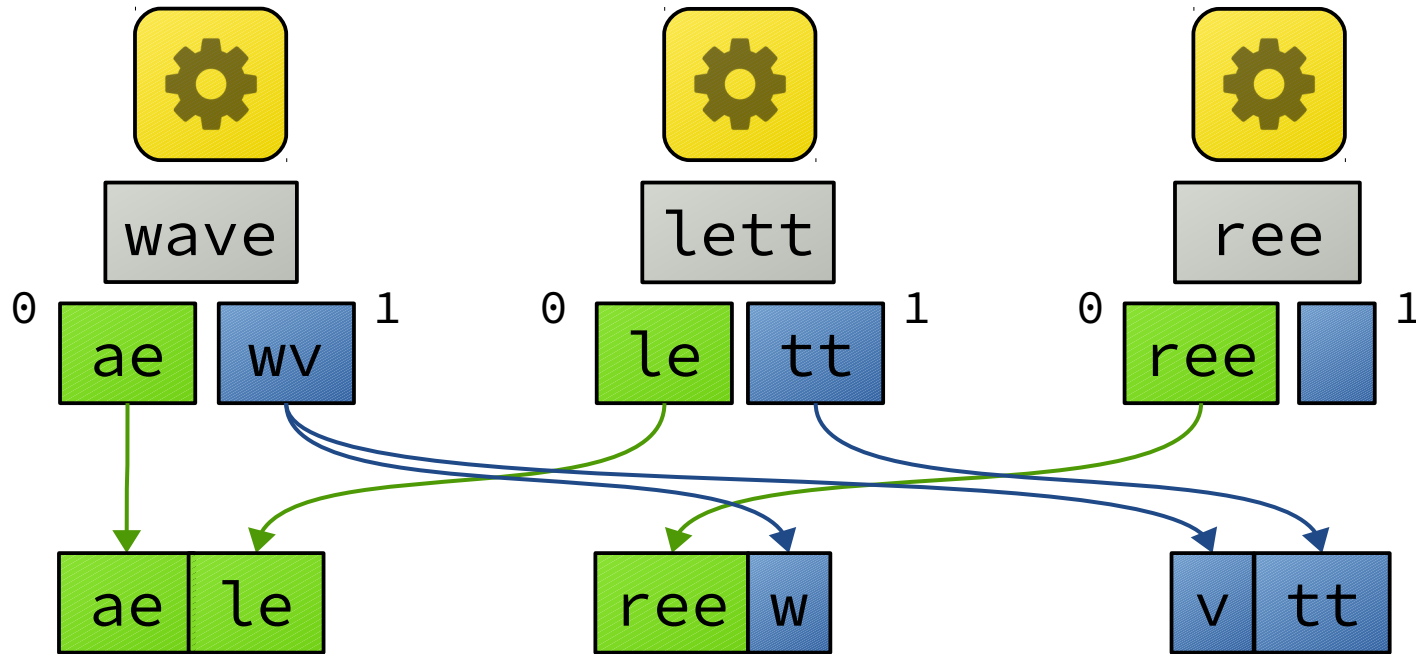
Stabiles Sortieren

Verteilter Bucket Sort



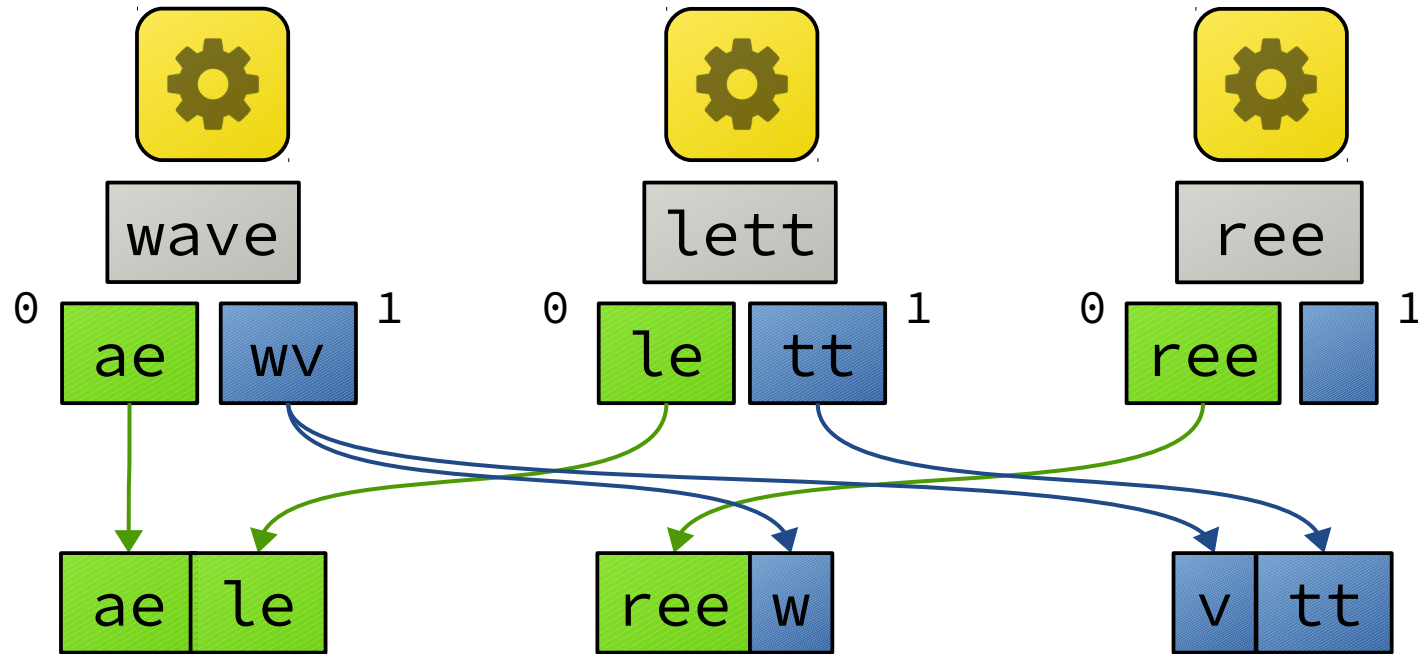
Stabiles Sortieren

Verteilter Bucket Sort



Stabiles Sortieren

Verteilter Bucket Sort



→ *Levelweise Domain Decomposition!*

Übersicht BSP-Kosten

$\mathcal{O}(\dots)$



DD

Split

$$p\sigma + n \log \sigma + H(\text{DD})$$

Sort

Übersicht BSP-Kosten

$\mathcal{O}(\dots)$



DD $W(\text{localWT}) + \sigma \log p + \sigma \frac{n}{p}$

Split $n\sigma + \sigma \log p + \sigma \frac{n}{p}$

Sort $\frac{n}{p} \log \sigma + \sigma \log p + \sigma \frac{n}{p}$

$p\sigma + n \log \sigma + H(\text{DD})$

Übersicht BSP-Kosten

$\mathcal{O}(\dots)$

			
DD	$W(\text{localWT}) + \sigma \log p + \sigma \frac{n}{p}$	$p\sigma + n \log \sigma$	
Split	$n\sigma + \sigma \log p + \sigma \frac{n}{p}$	$p\sigma + n \log \sigma + H(\text{DD})$	
Sort	$\frac{n}{p} \log \sigma + \sigma \log p + \sigma \frac{n}{p}$	$p\sigma + n \log \sigma$	

Übersicht BSP-Kosten

$\mathcal{O}(\dots)$

			
DD	$W(\text{localWT}) + \sigma \log p + \sigma \frac{n}{p}$	$p\sigma + n \log \sigma$	$\log p + \log \sigma$
Split	$n\sigma + \sigma \log p + \sigma \frac{n}{p}$	$p\sigma + n \log \sigma + H(\text{DD})$	$\log(p) \log(\sigma) + S(\text{DD})$
Sort	$\frac{n}{p} \log \sigma + \sigma \log p + \sigma \frac{n}{p}$	$p\sigma + n \log \sigma$	$\log(p) \log(\sigma)$

Implementierung



Implementierung



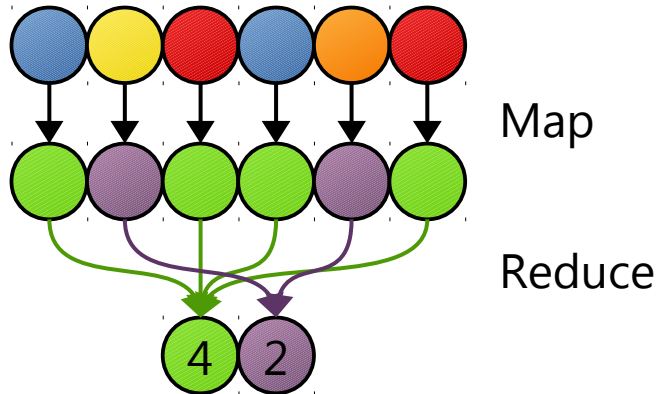
Thrill

- Framework in C++14
- Distributed Immutable Arrays
- Datenflussbasierte High-Level-Operationen auf Sequenzen

Implementierung

Thrill

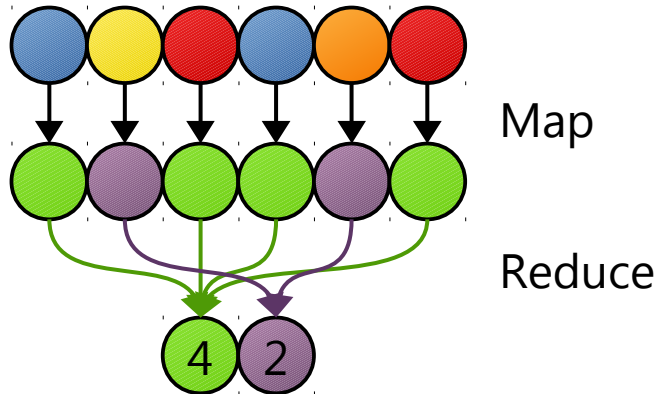
- Framework in C++14
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Implementierung

Thrill

- Framework in C++14
- Distributed Immutable Arrays
- Datenflussbasierte High-Level-Operationen auf Sequenzen



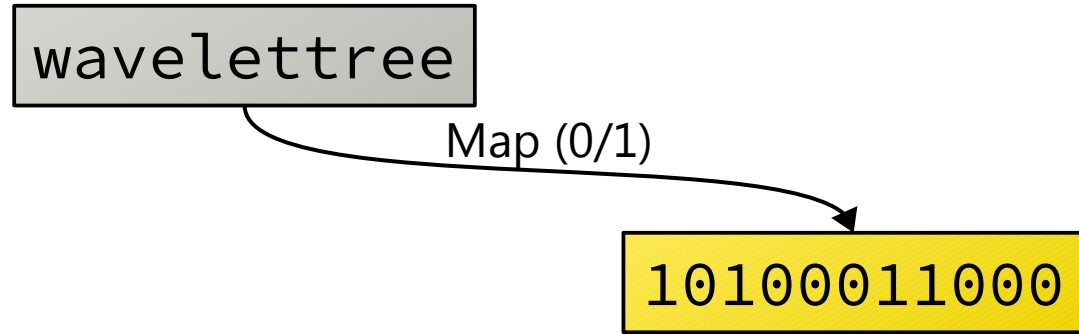
MPI (Message Passing Interface)

- C-Bibliothek
- Low-Level-Schnittstelle zum Nachrichtenaustausch
- Primitive: Send / Recv / Probe
- Komplex: Allreduce, Exscan

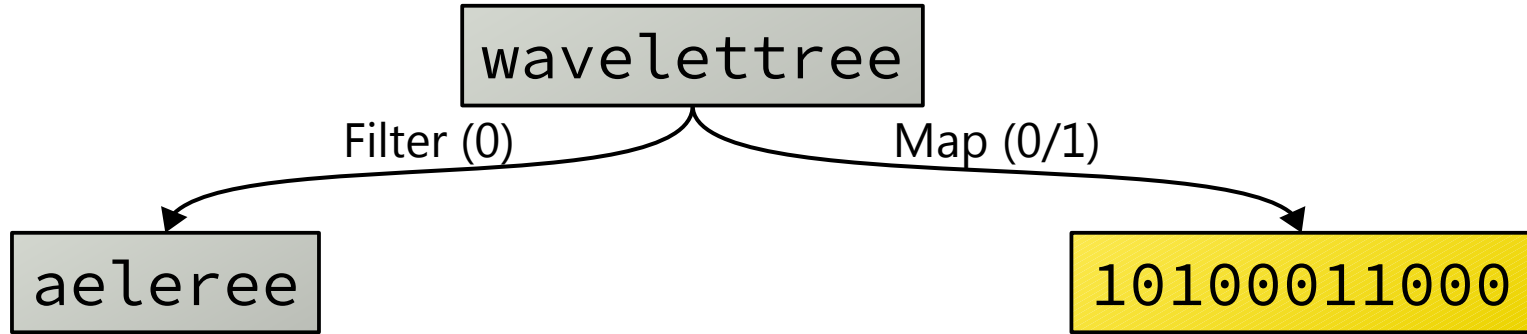
Thrill

wavelettree

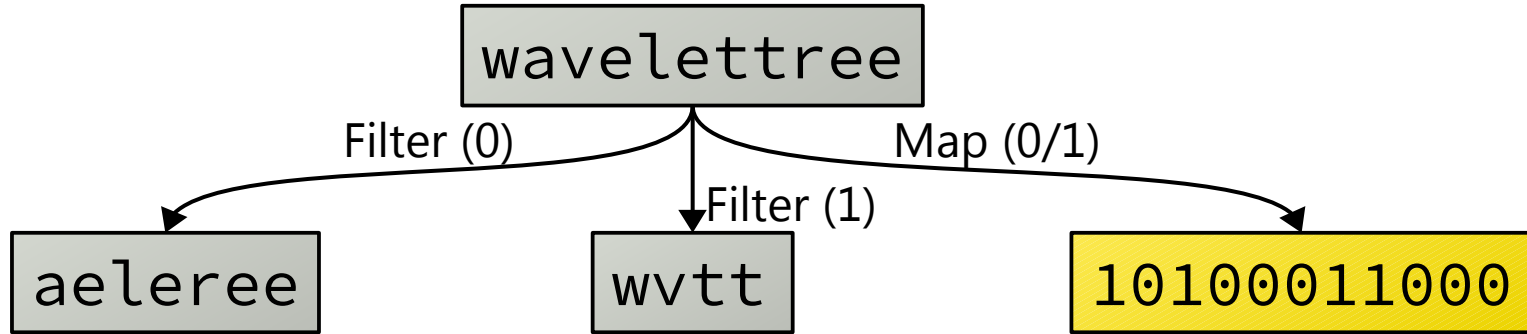
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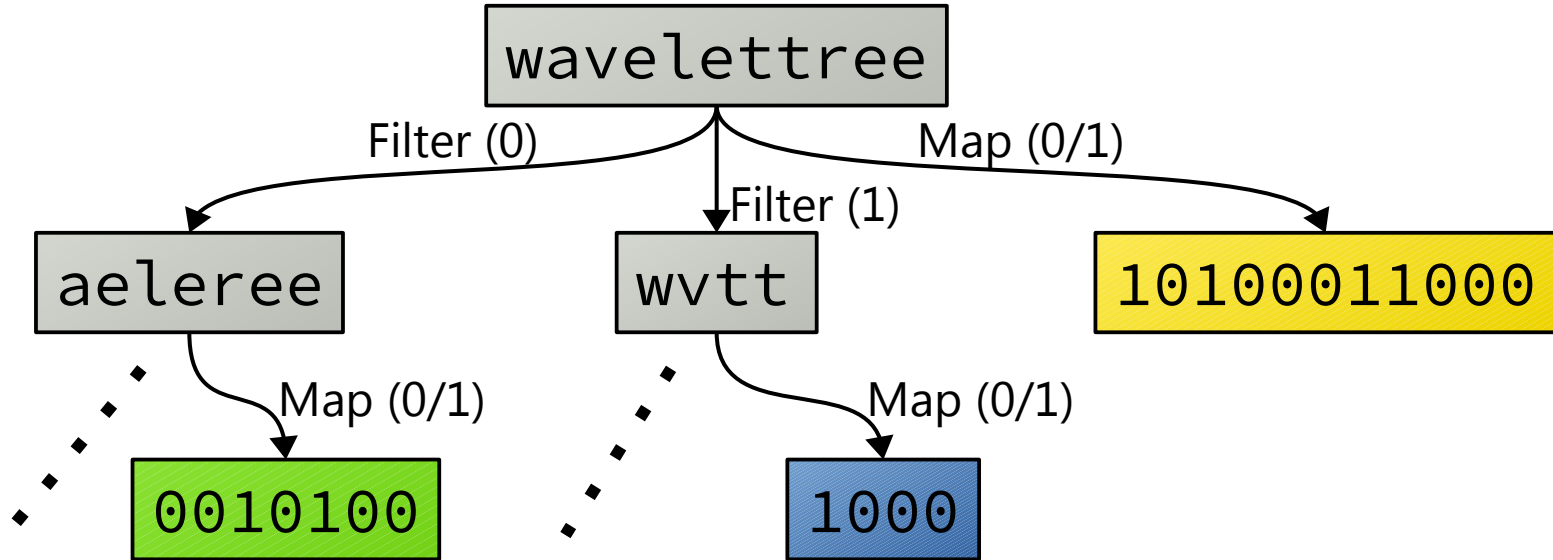
Thrill



Thrill

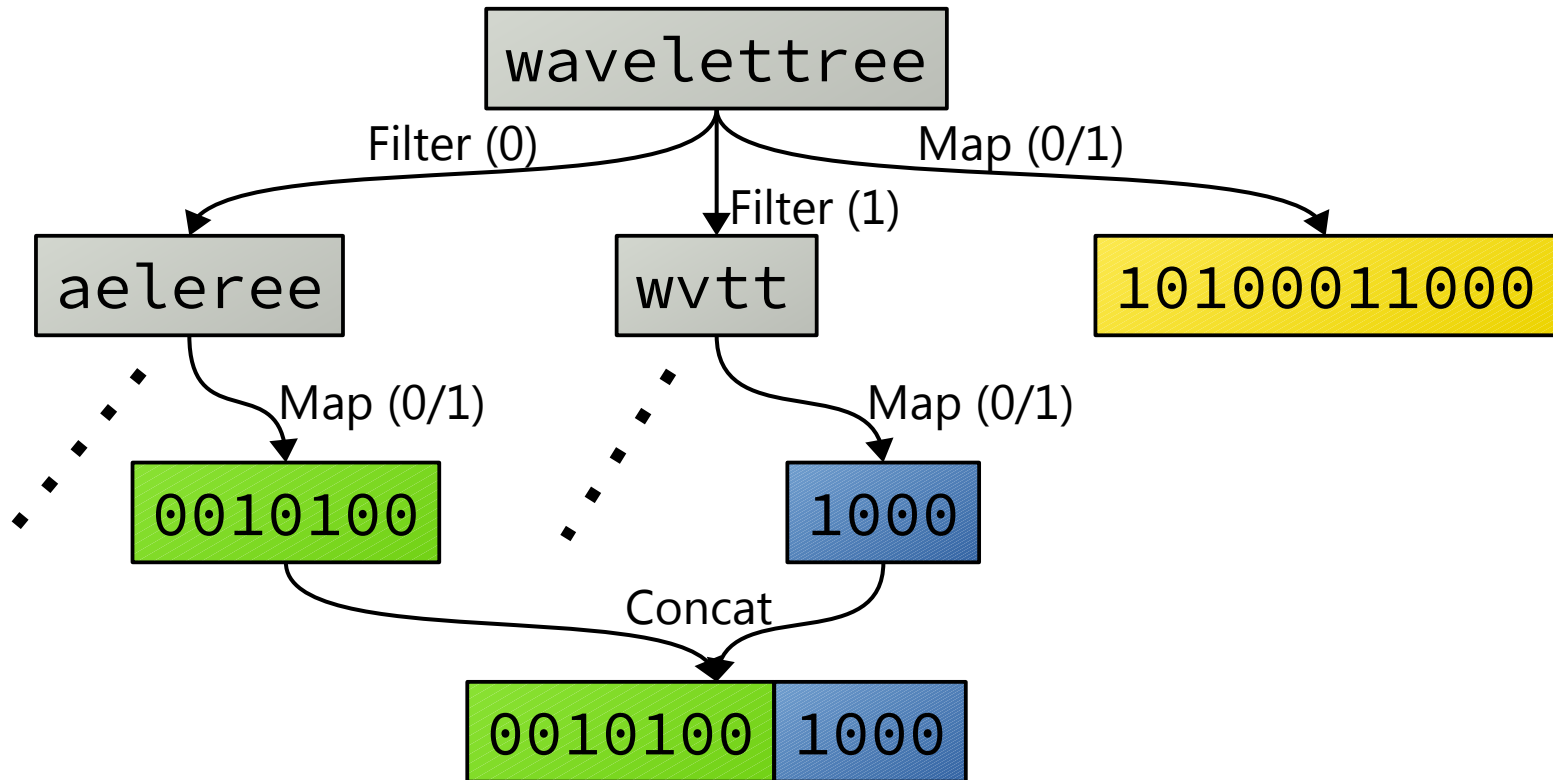


Thrill



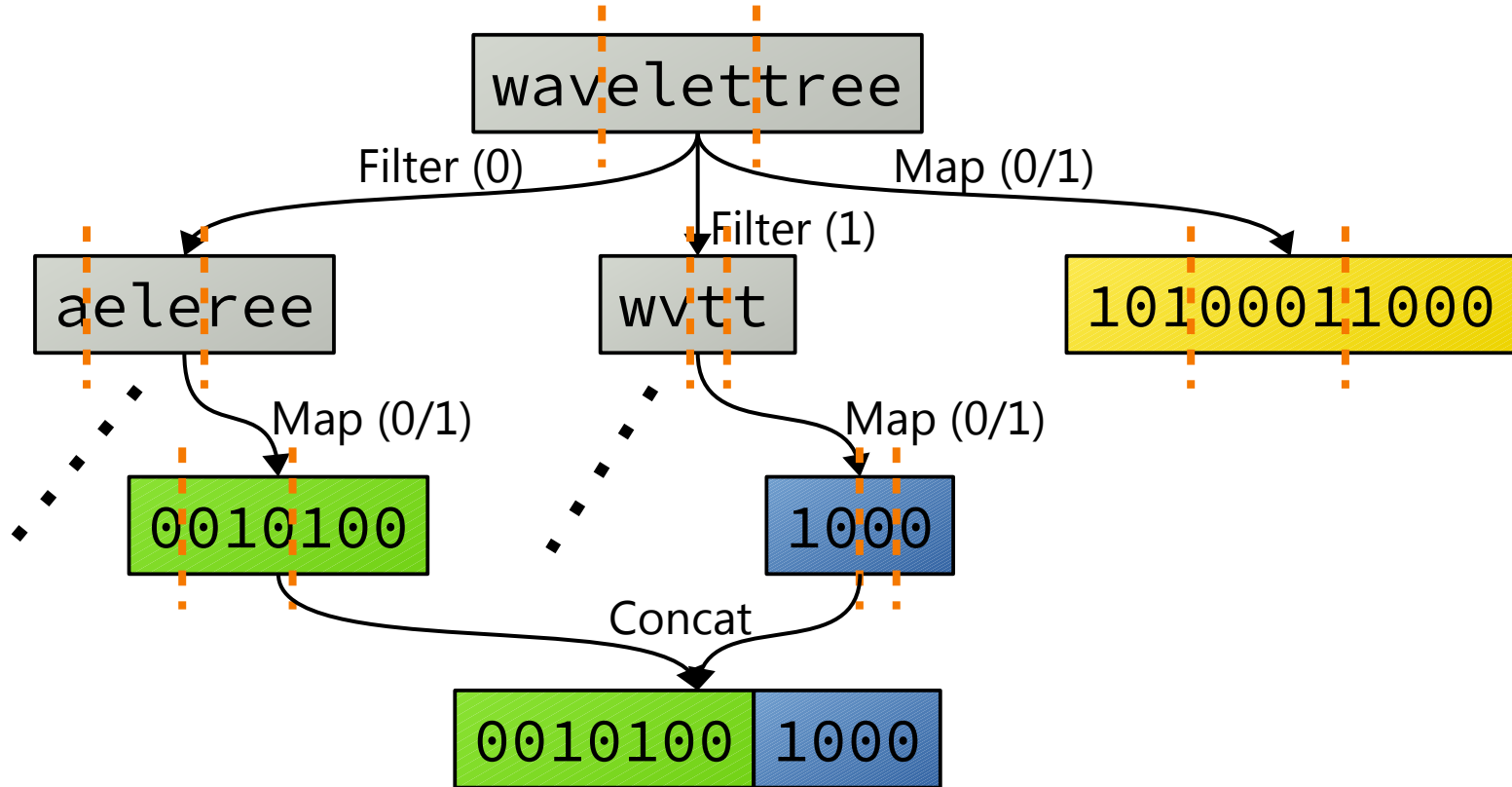
Thrill

Domain Decomposition

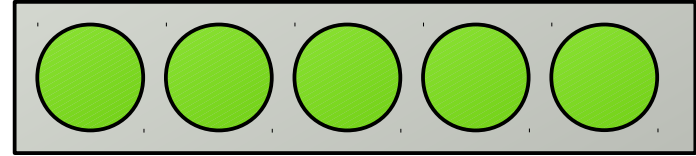
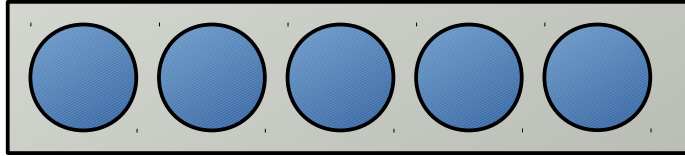


Thrill

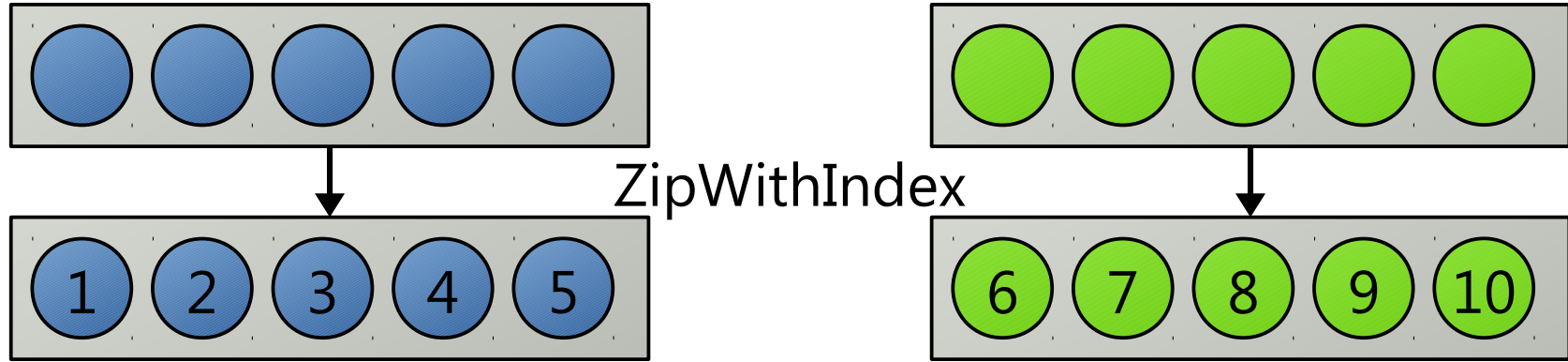
Domain Decomposition



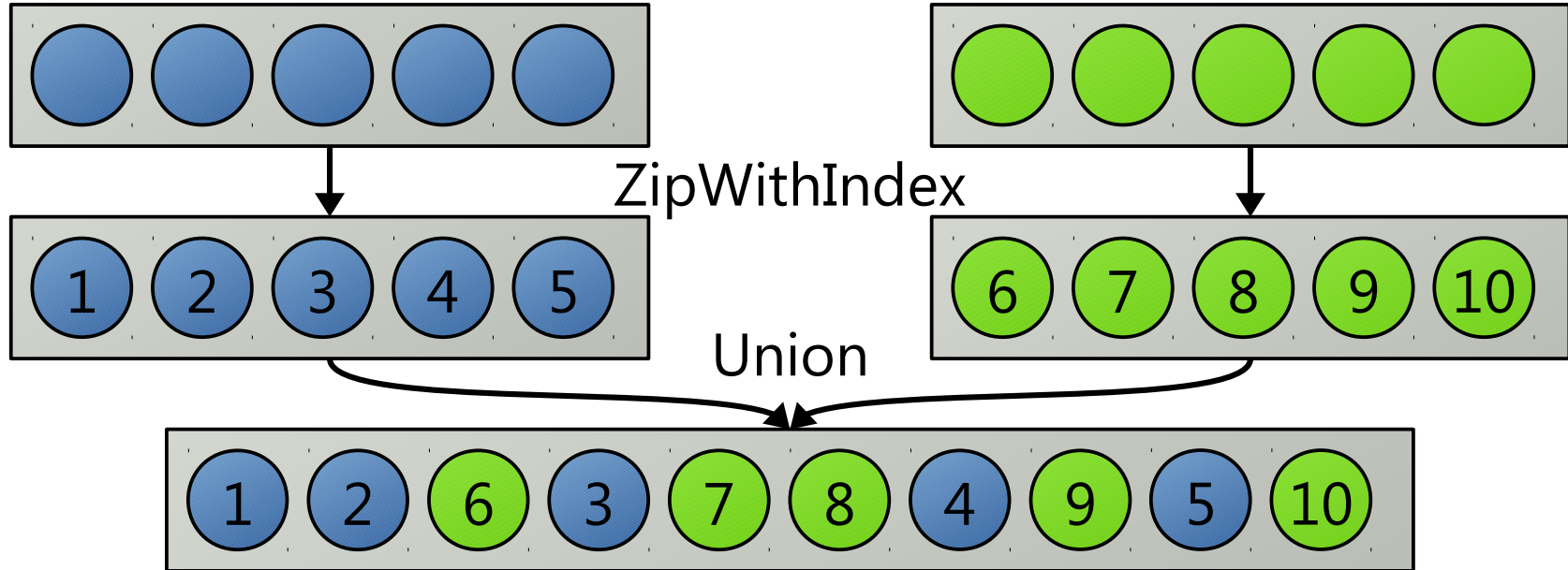
Concat in Thrill



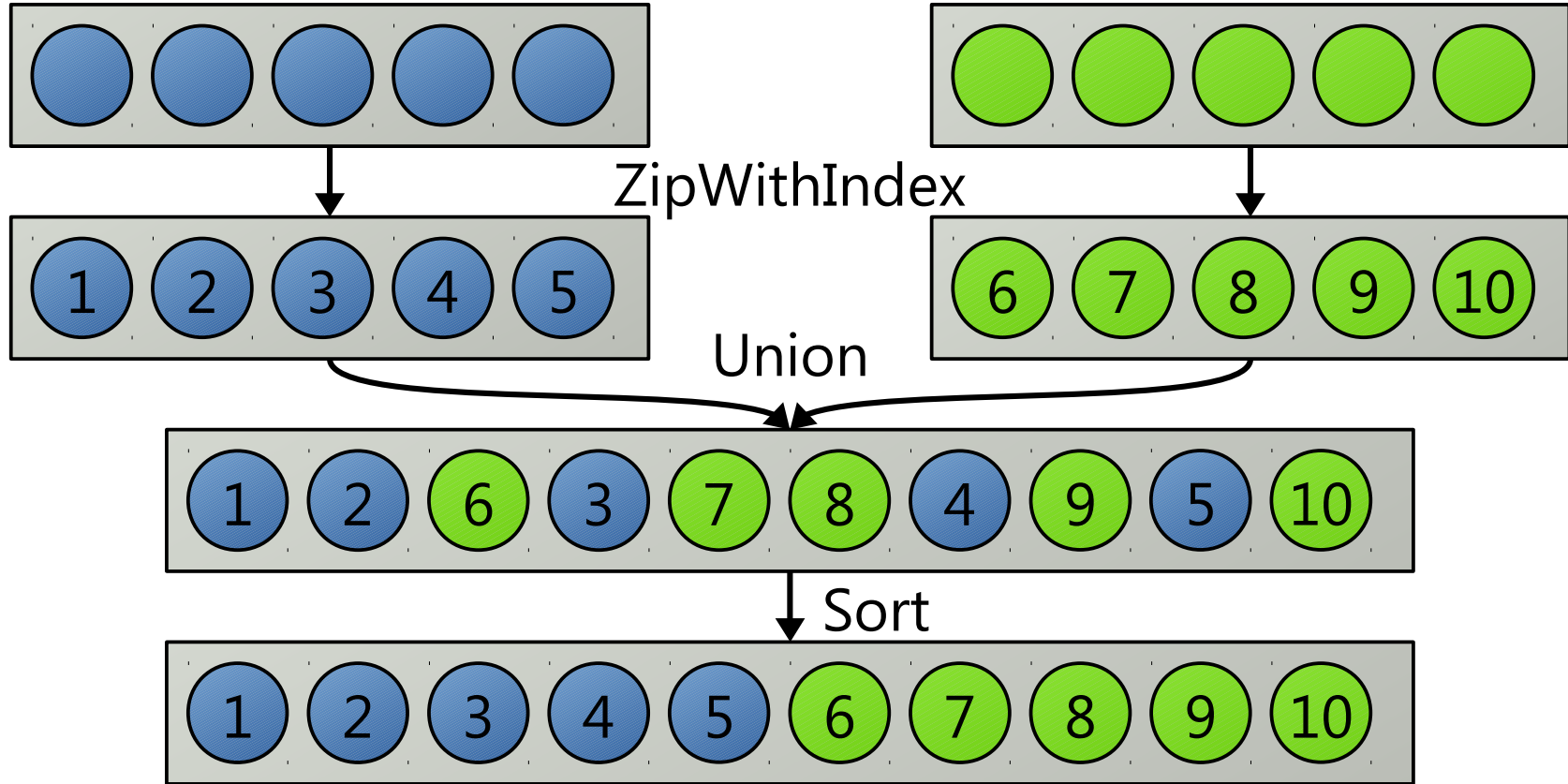
Concat in Thrill



Concat in Thrill



Concat in Thrill



Concat in Thrill

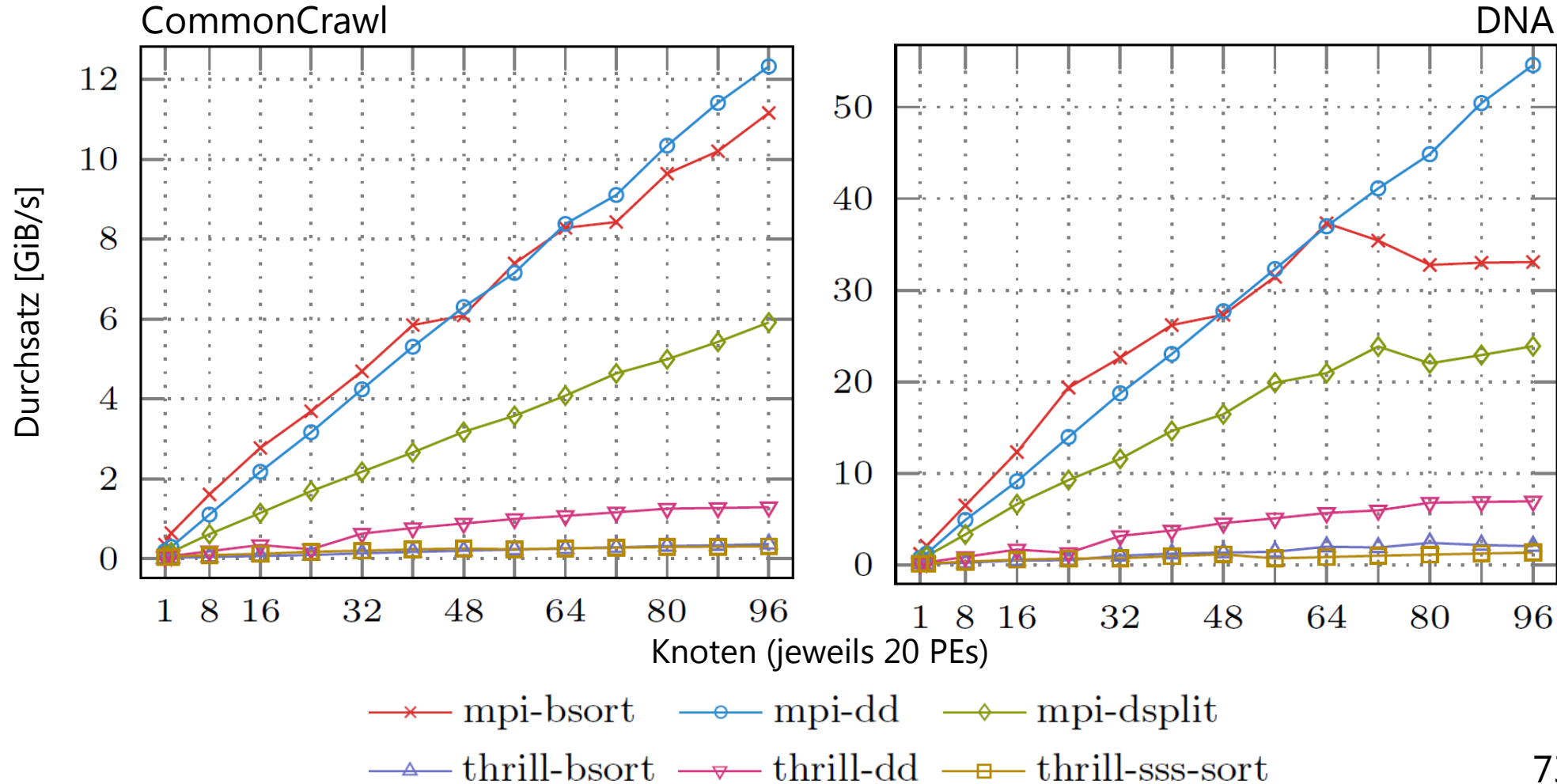


Evaluation

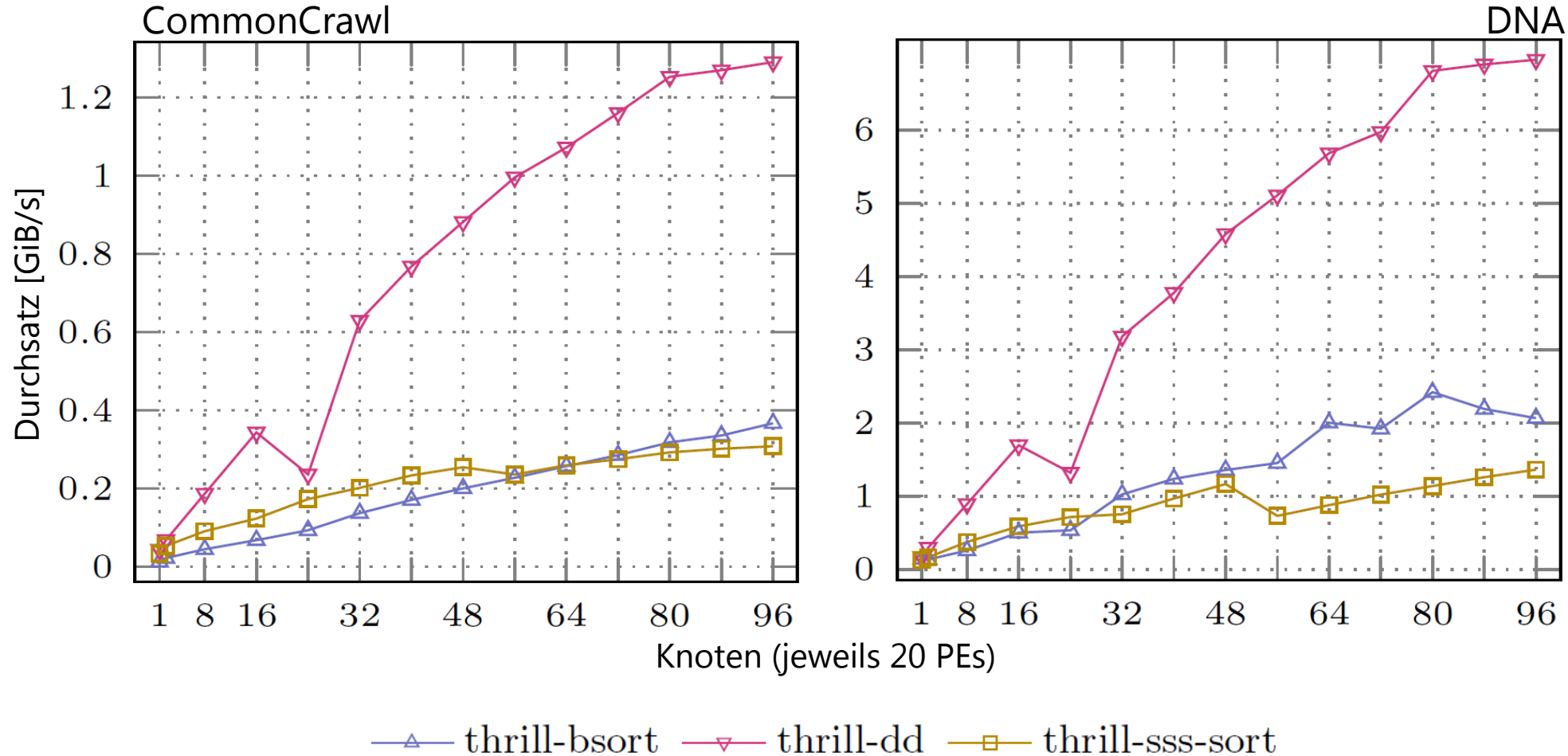
Weak-Scaling-Experimente

- LiDO3-Cluster (20 PEs je Knoten)
- CommonCrawl ($\sigma=242 \rightarrow 8$ WT-Level)
- DNA ($\sigma=4 \rightarrow 2$ WT-Level)
- 1 GiB je Knoten
- Thrill- und MPI-Implementierungen

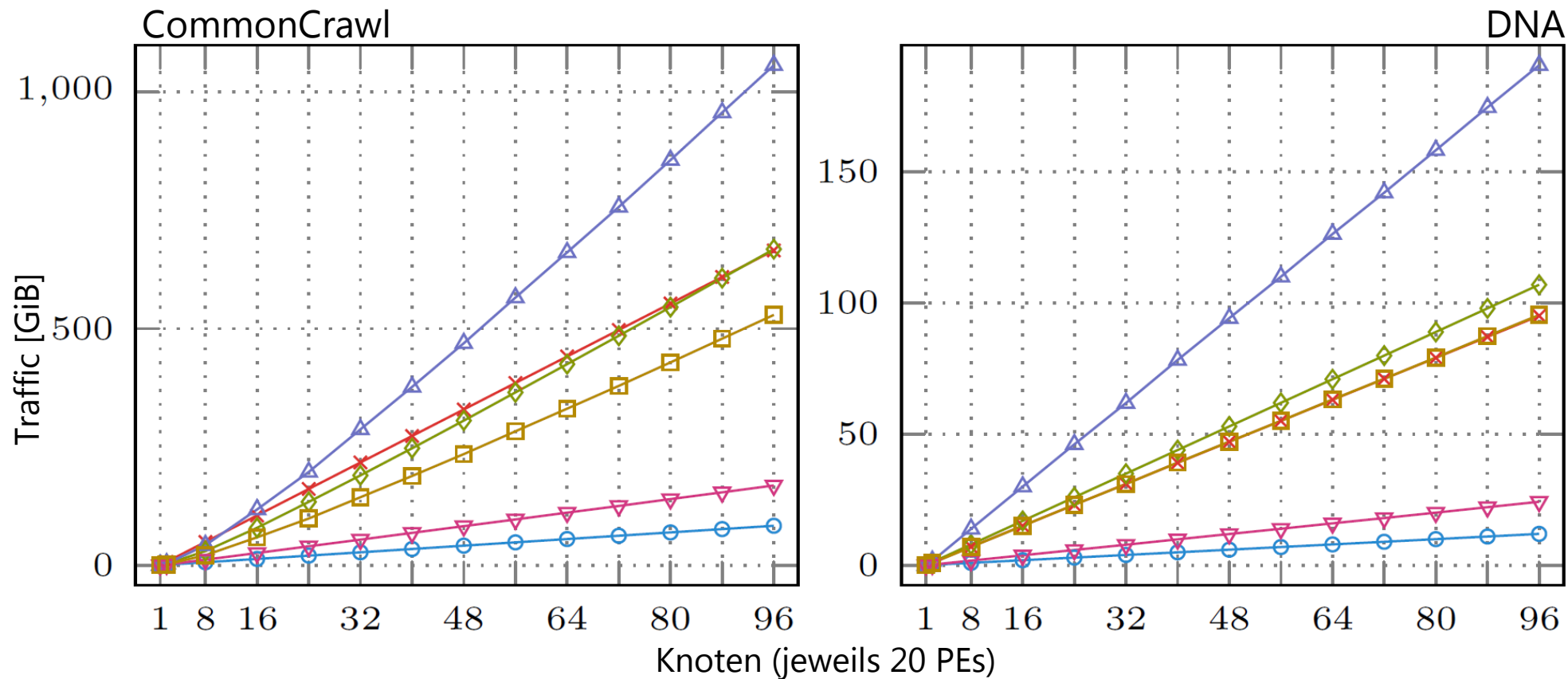
Weak Scaling – Durchsatz



Weak Scaling – Durchsatz (Thrill)

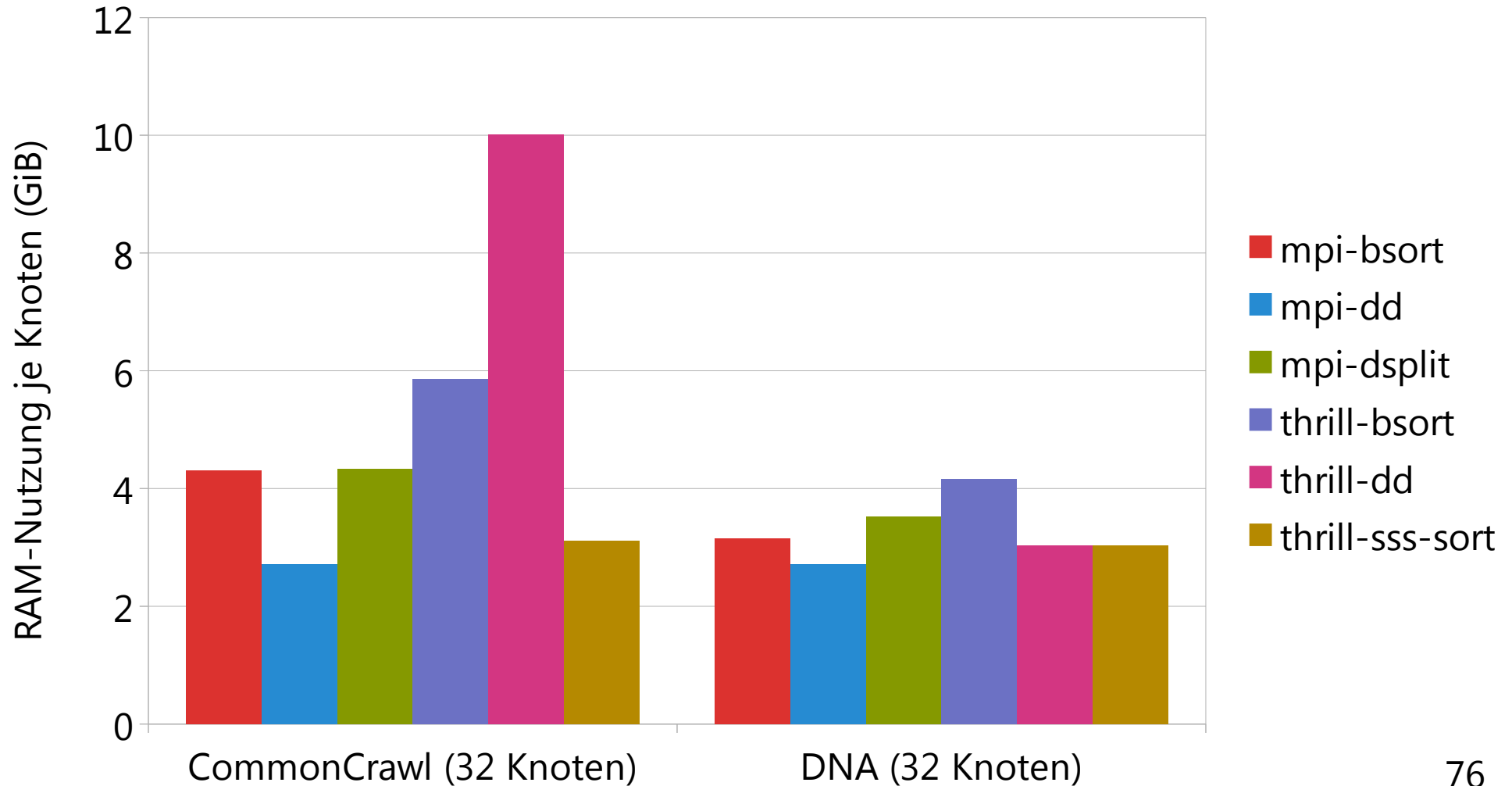


Weak Scaling - Traffic



—x— mpi-bsort —○— mpi-dd —◇— mpi-dsplt
—△— thrill-bsort —▽— thrill-dd —□— thrill-sss-sort

Weak Scaling - Speichernutzung



Fazit

- Verteilte WT-Konstruktion skaliert im Allgemeinen recht gut
- Domain Decomposition skaliert nahezu perfekt und benötigt den geringsten Traffic und Speicherplatz